

Multiwalled carbon nanotubes: the thicker, the softer



IJIMA ET AL. (1996)

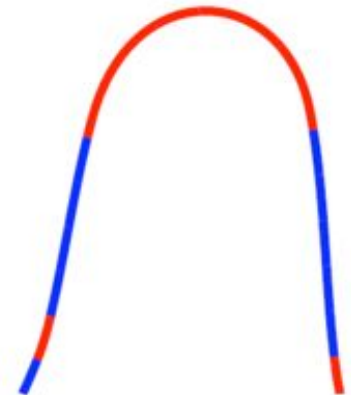


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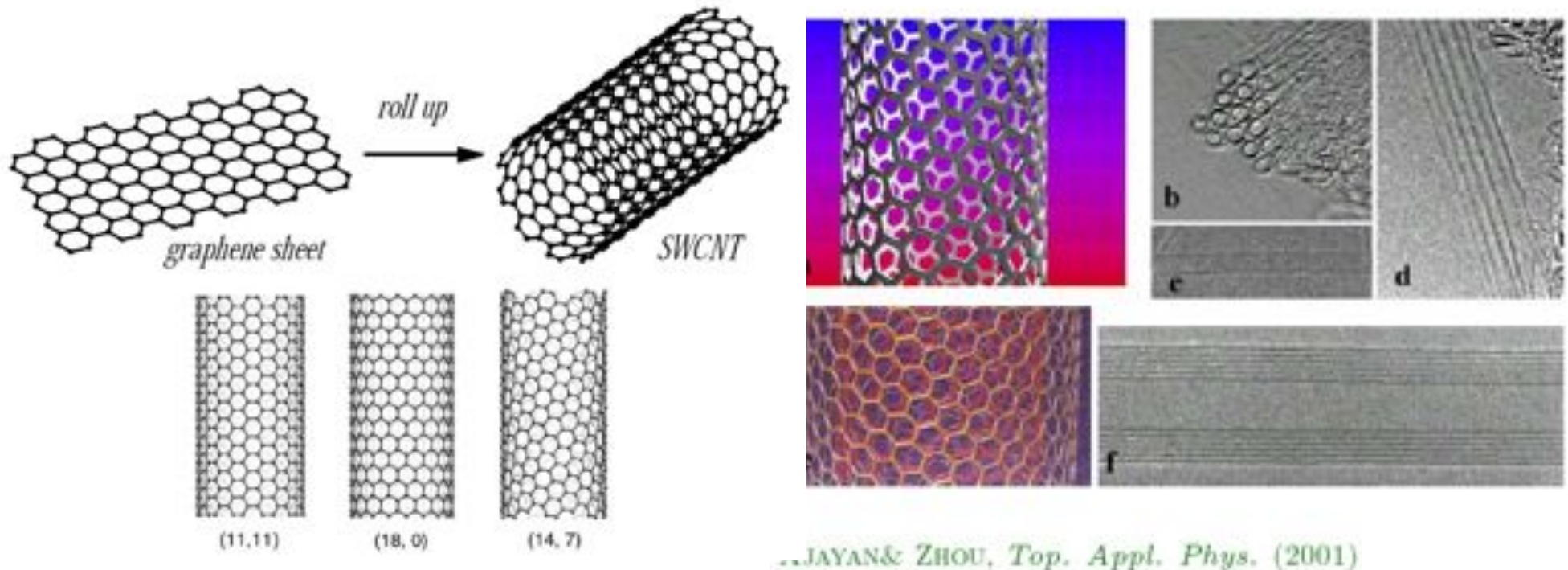
Universitat Politècnica de Catalunya (Spain)

NanoSpain'09, Zaragoza, 2009



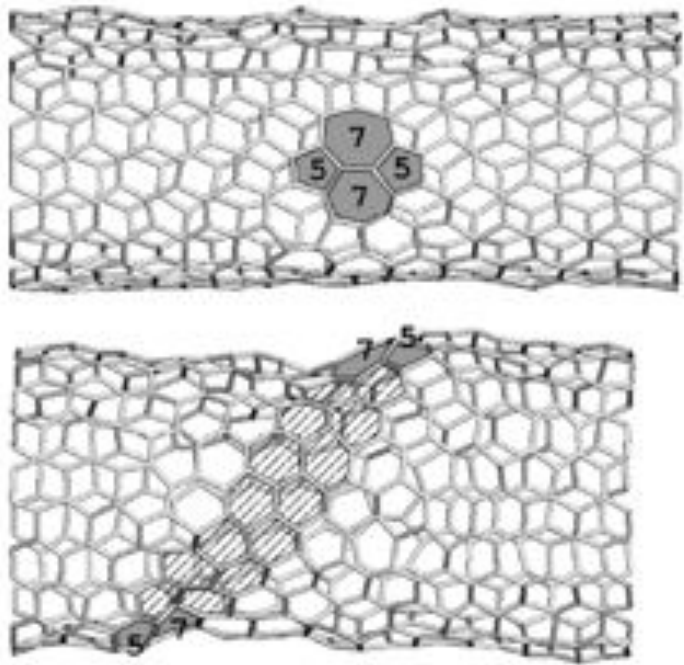
Introduction: CNTs Mechanics

CNTs come alone (SWCNTs), in bundles, or nested (MWCNTs).

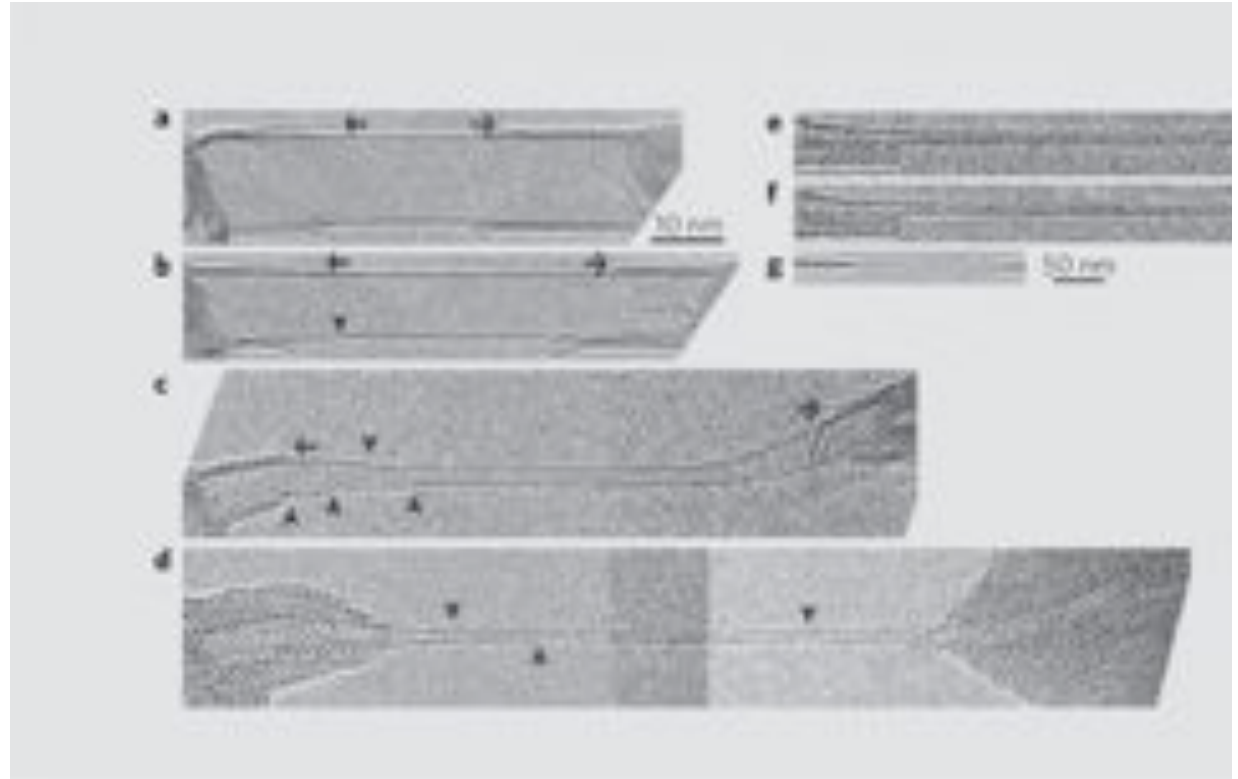


Unique structure and size, together with remarkable mechanical, electronic, thermal, chemical properties make them attractive in nanostructured materials and devices.

Introduction: CNTs Mechanics



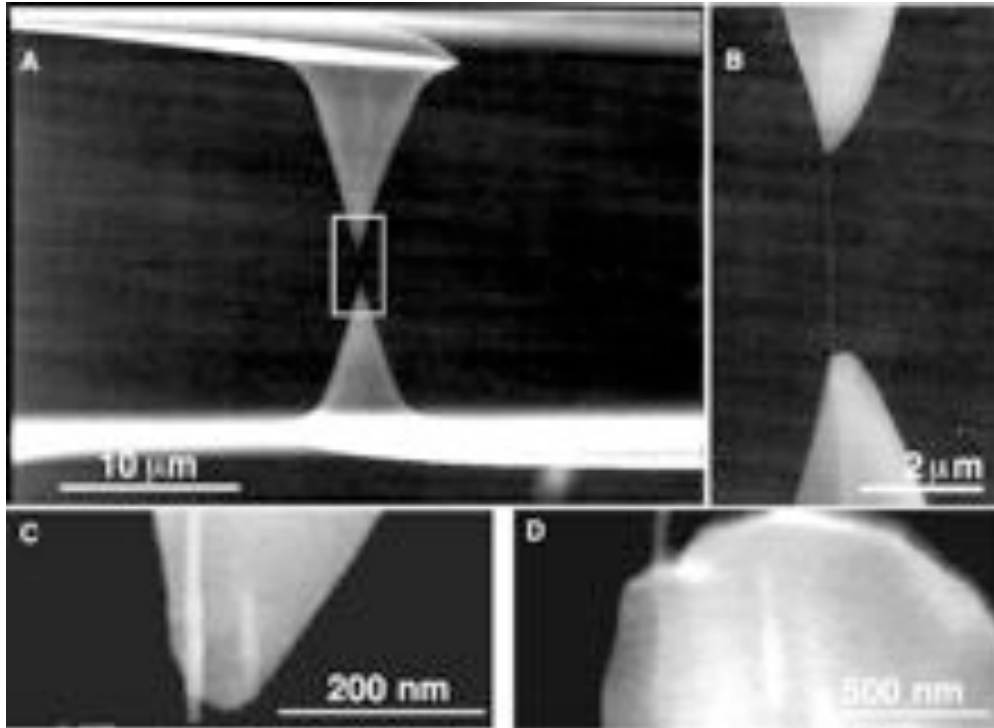
Nardelli et al, *PRL* (1996)



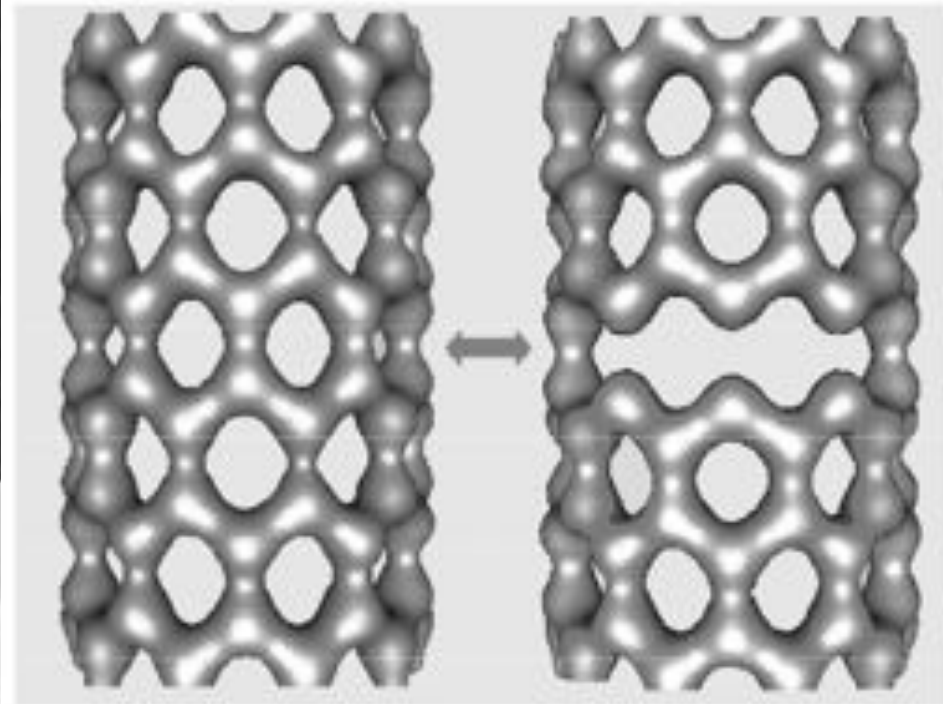
Huang et al, *Nature* (2006)

CNTs can experience plasticity at high temperatures...

Introduction: CNTs Mechanics



Yu et al, *Science* (2000)



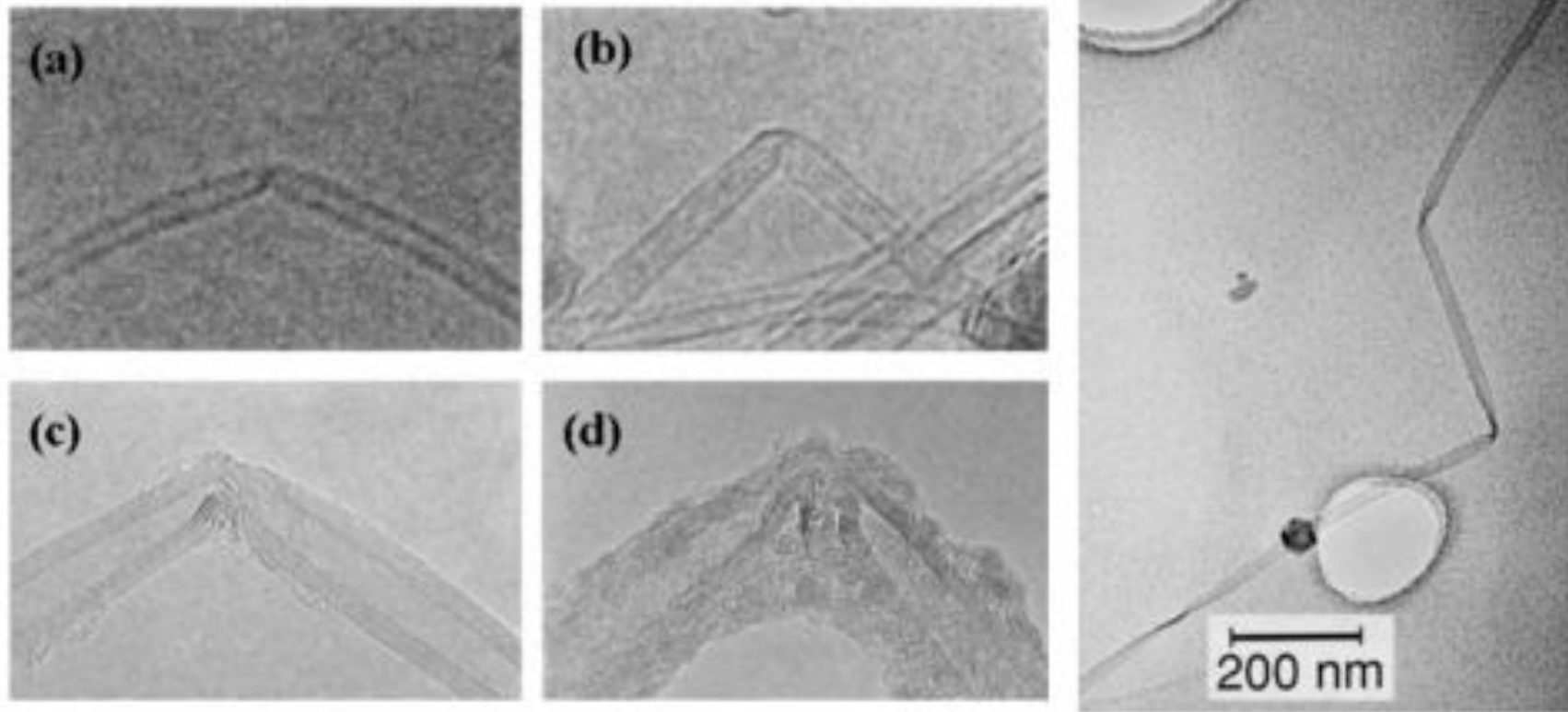
Dumitrica et al, *J. Chem. Phys* (2003)

or fracture at room temperature...

Introduction: CNTs Mechanics

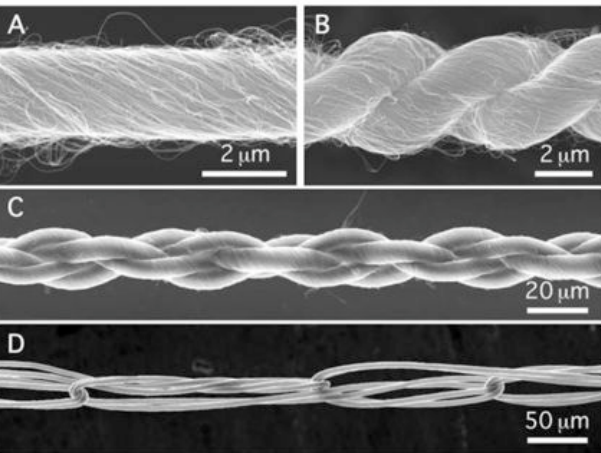
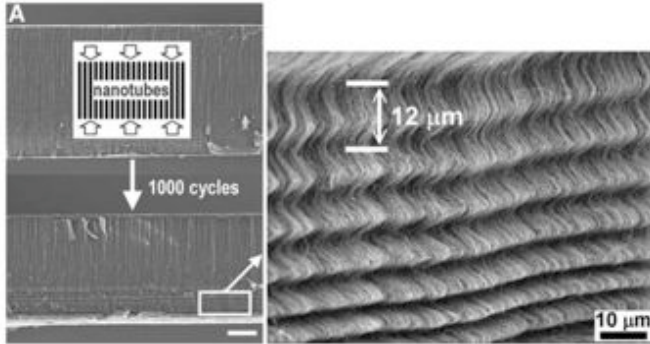
Because of the hollow geometry and crystalline perfection and stability, they are extremely resilient and undergo **reversibly** very large deformations with buckling.

Very rich nonlinear elasticity



Multiscale mechanics

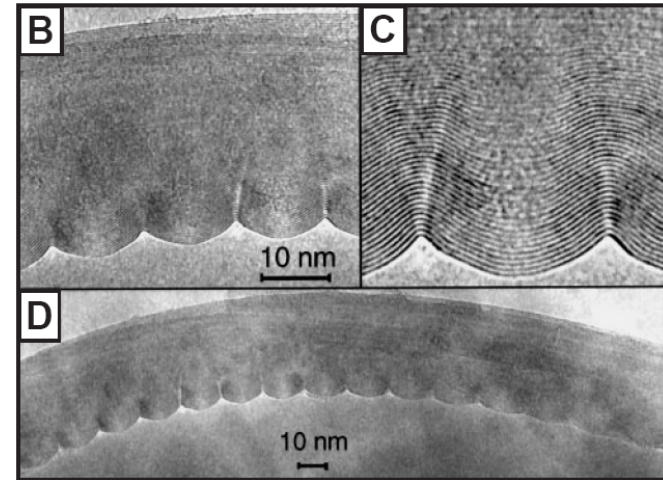
Cao et al, *Science* (2005)



Baughman et al, *Science* (2004)
10's of microns

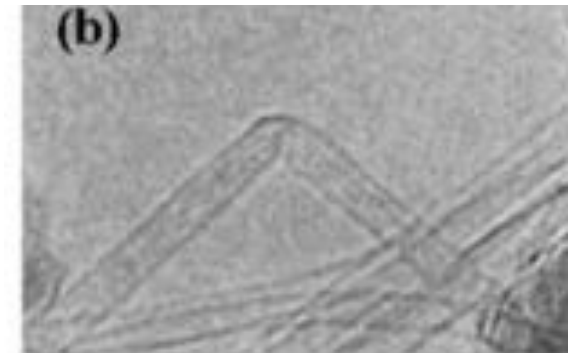


Baughman et al, *Science* (2002)
Amstrongs



Poncharal et al, *Science* (1999)
100's of nanometers

Build large scale models
from microscopic models
to reduce empiricism and
uncertainty



Iijima et al (1996)
nanometers

Multiple-scale analysis

Continuum surface models from atomistic models *Arroyo & Belytschko, JMPS (2002)*

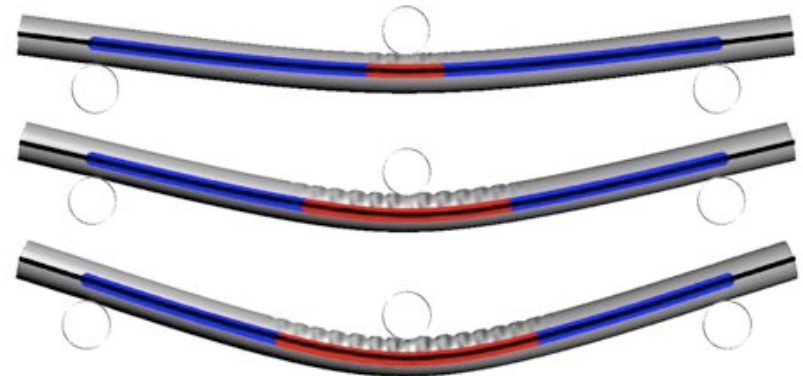
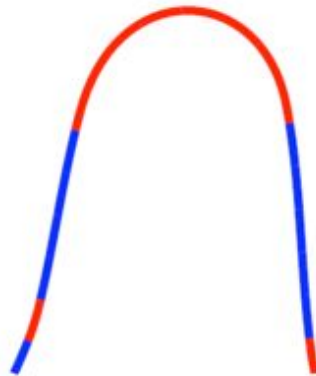


Mechanics of thick multiwalled CNTs through scaling laws



Mesoscopic models, phase-transforming elastica

(LaCàN•)



Mechanics of thick MWCNTs

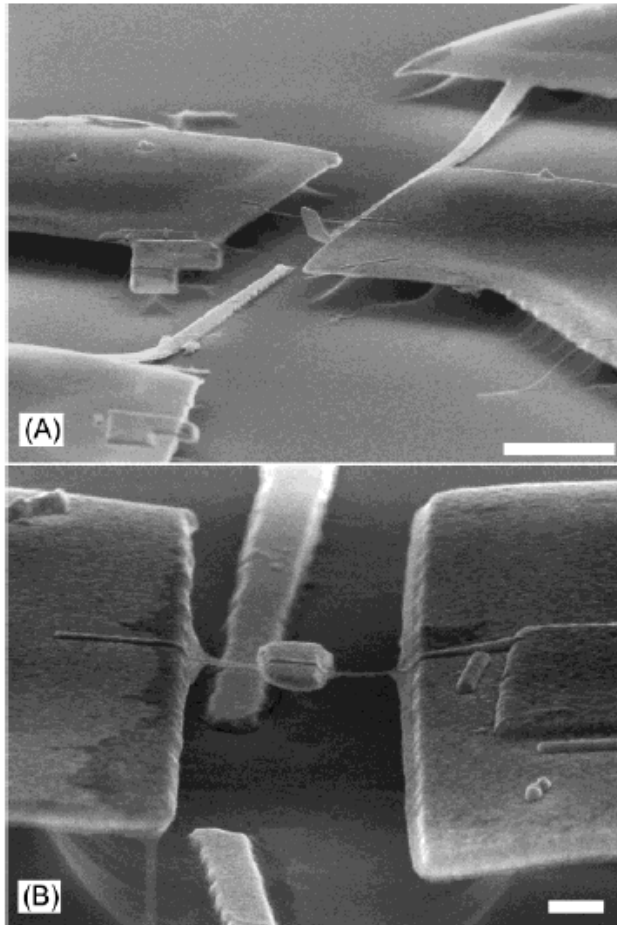
I. Arias and M. Arroyo, Size-dependent nonlinear elastic scaling of multiwalled carbon nanotubes, *Physical Review Letters*, 100:085503 (2008).



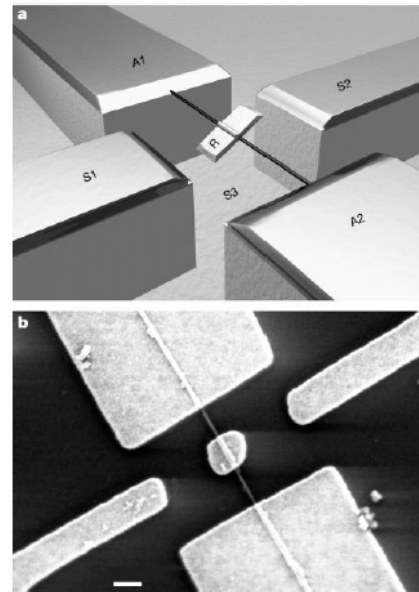
Mechanics of thick MWCNTs

Thick MWCNTs are central in a number of nanodevices and materials

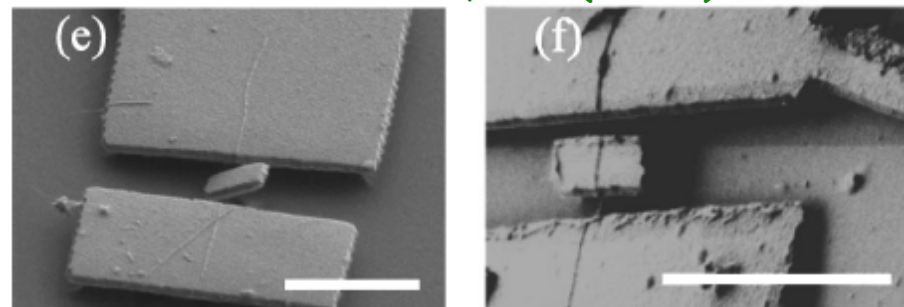
Bournlon et al, Nanoletters (2004)



Fennimore et al, Nature (2003)

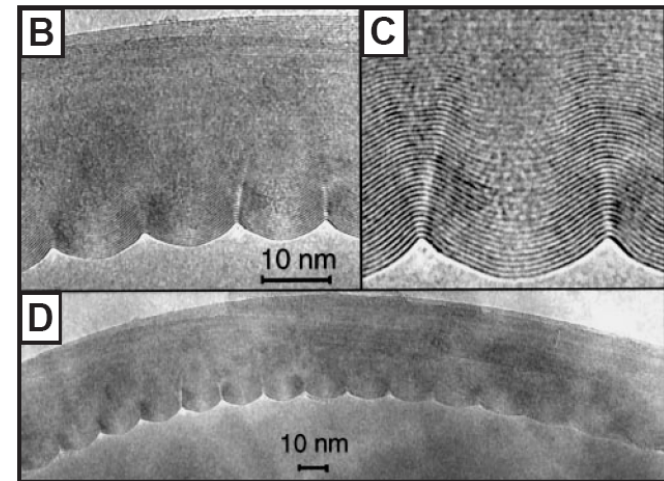
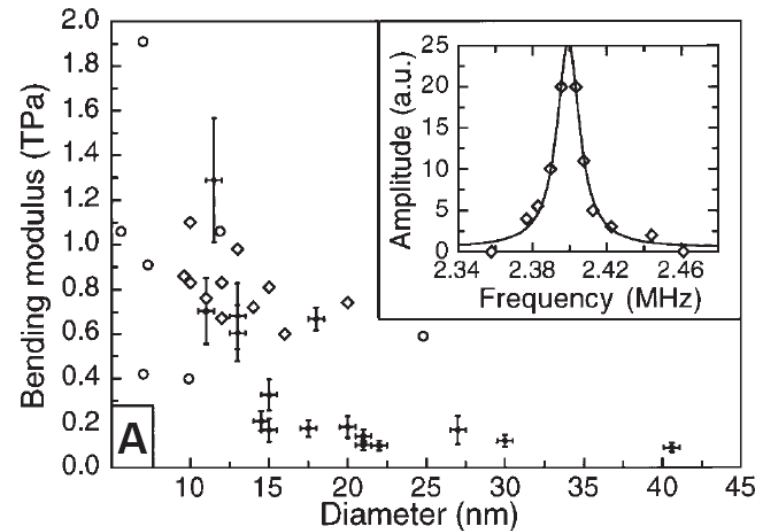
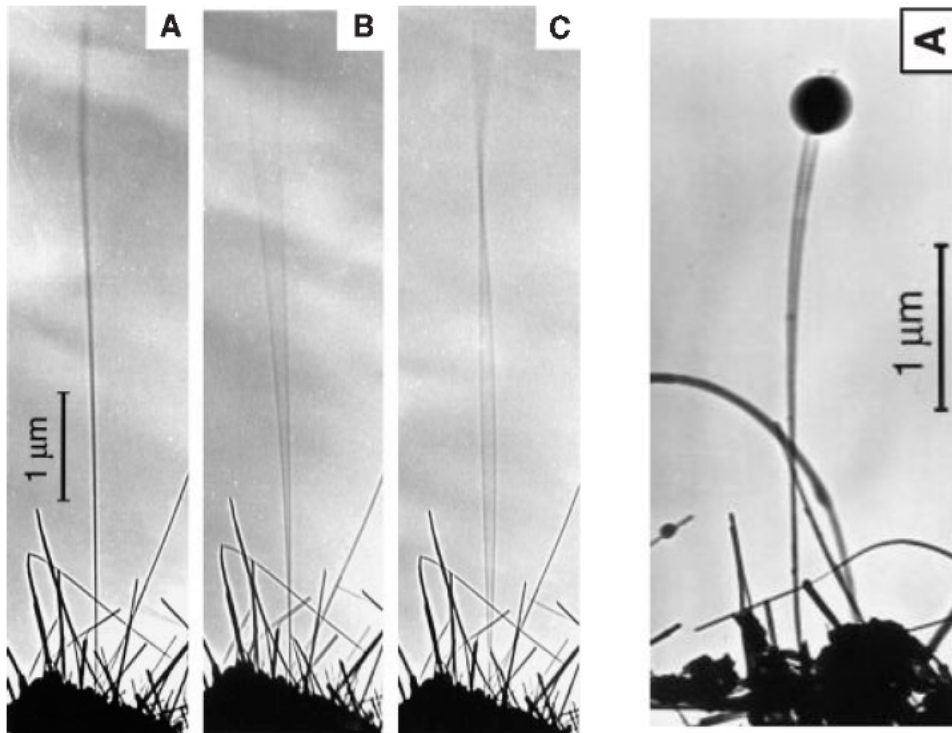


Williams et al, PRL (2003)



Mechanics of thick MWCNTs

Thick MWCNTs are central in a number of nanodevices and materials

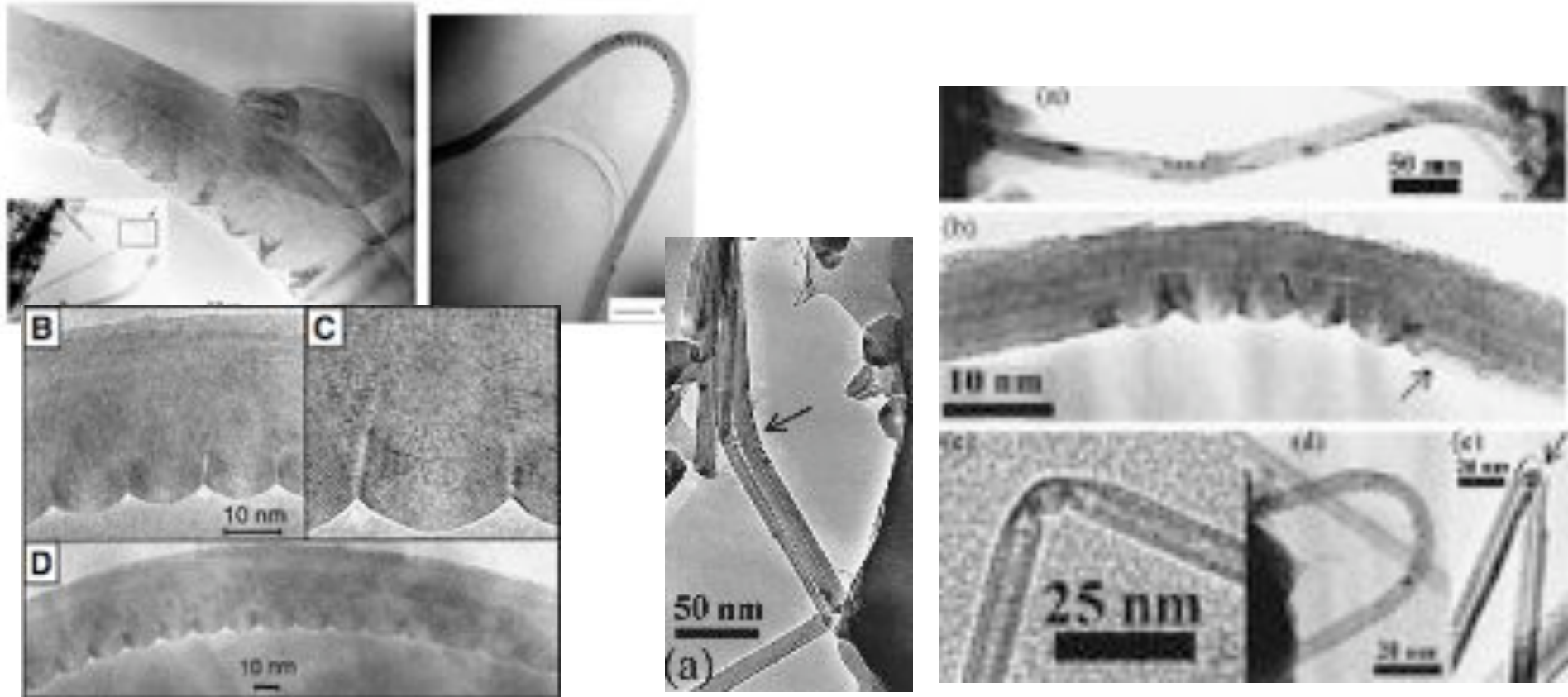


$$v_j = \frac{\beta_j^2}{8\pi} \frac{1}{L^2} \sqrt{(D^2 + D_i^2)} \sqrt{\frac{E_b}{\rho}}$$

Poncharal et al, *Science* (1999)

Mechanics of thick MWCNTs

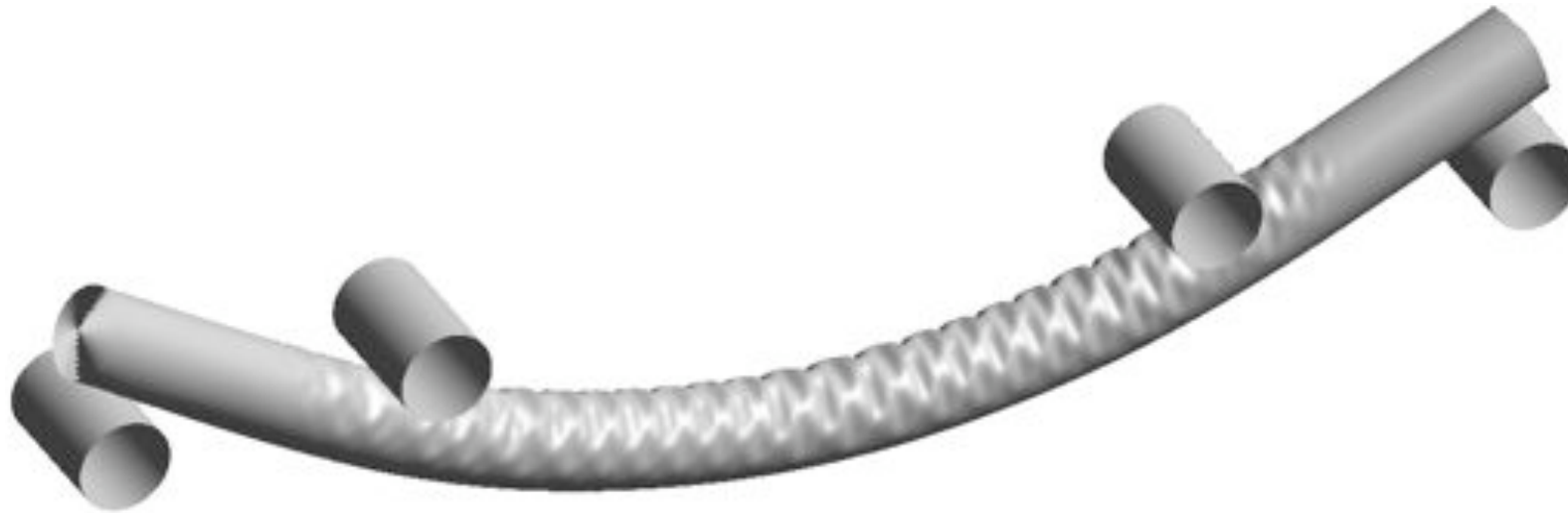
- In analyzing experiments, and modeling devices and materials, thick MWCNTs are usually modeled as *linear elastic beams*...



- Reliable simulations of these multi-million atom systems are prohibitive, **simplified unrealistic models instead**

Mechanics of thick MWCNTs

The method proposed in [Arroyo & Belytschko, *IJNME* \(2004\)](#) allows for realistic simulations by reducing the number of dofs by two orders of magnitude, which still require high-performance computing facilities



40-walled CNT 0.5 microns

long: system containing nominally 31 million atoms is modeled with 400 000 FE nodes and computed on 512 processors

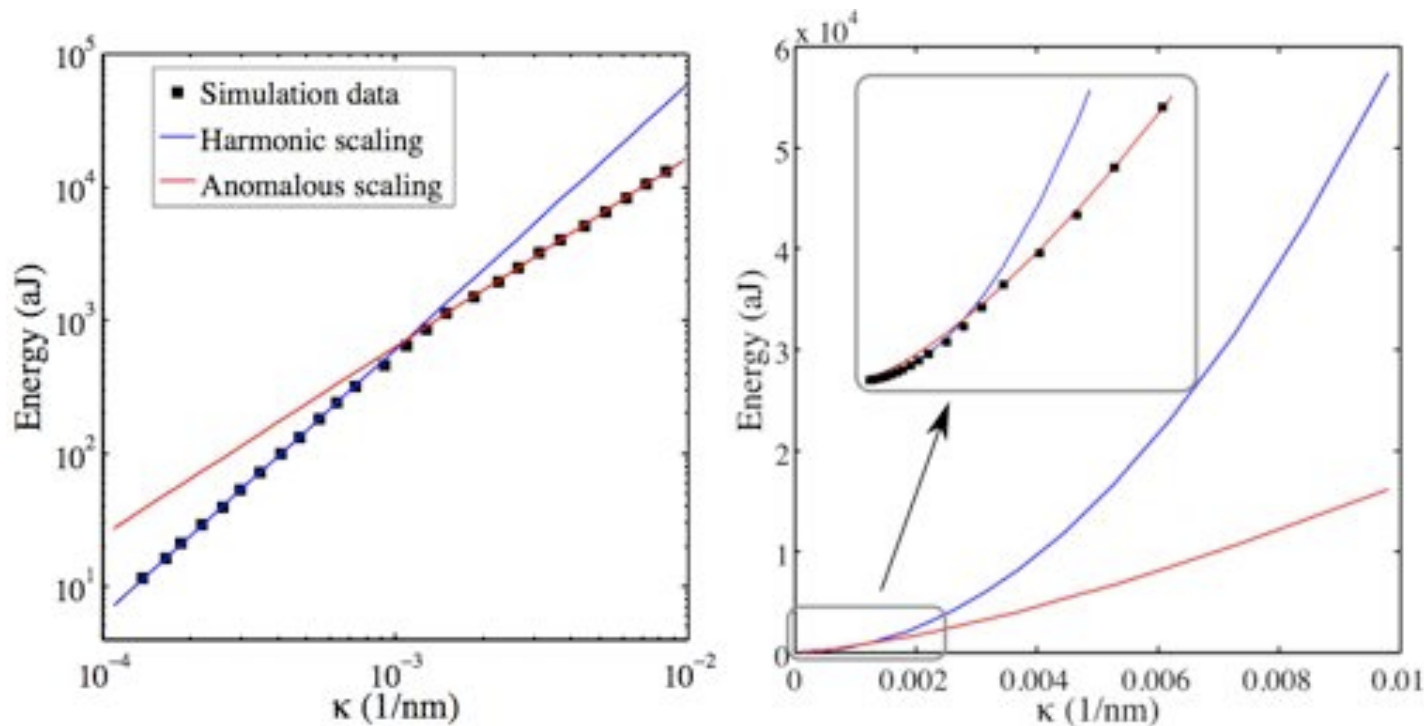


Mechanics of thick MWCNTs

Energy vs curvature relation has two regimes, it is a composite power law
(Arroyo & Belytschko, *PRL* 2003);

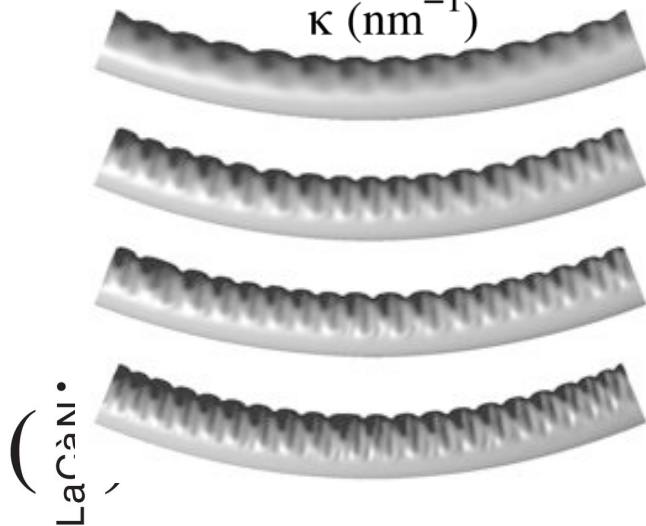
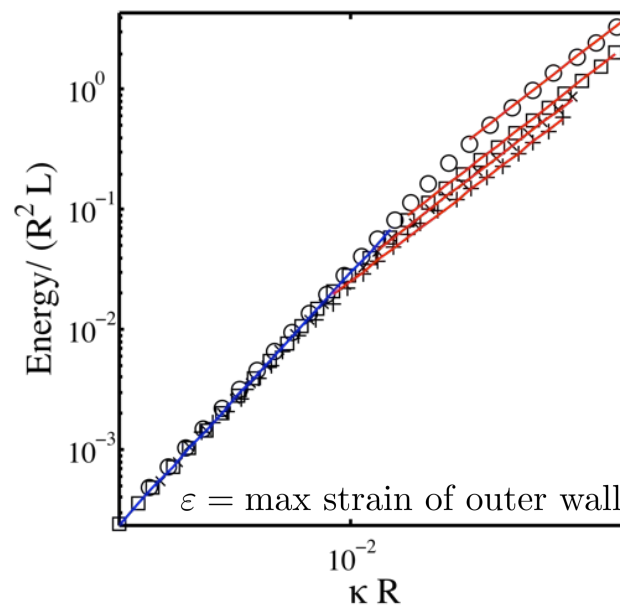
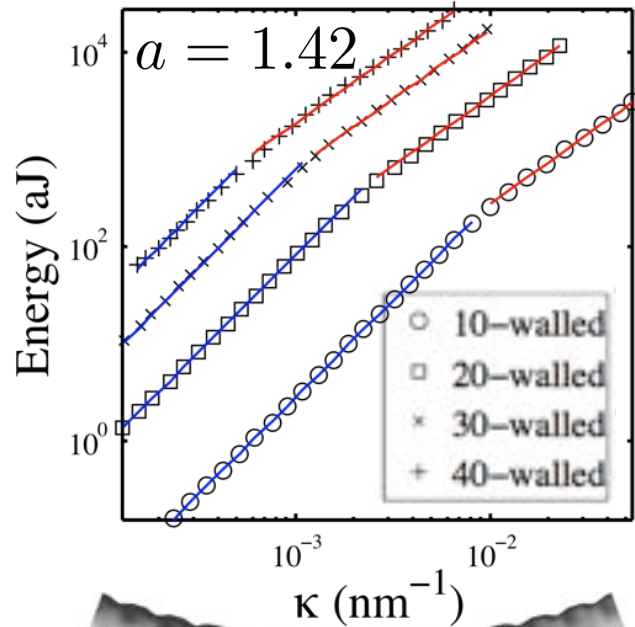
- The **harmonic regime** in which $E \sim \text{curvature}^2$
- An **anomalous elastic regime** with $E \sim \text{curvature}^\alpha$ and $1 < \alpha < 2$ for larger deformations, result of interplay of membrane, bending and vdW forces

This behavior is reversible with no significant hysteresis



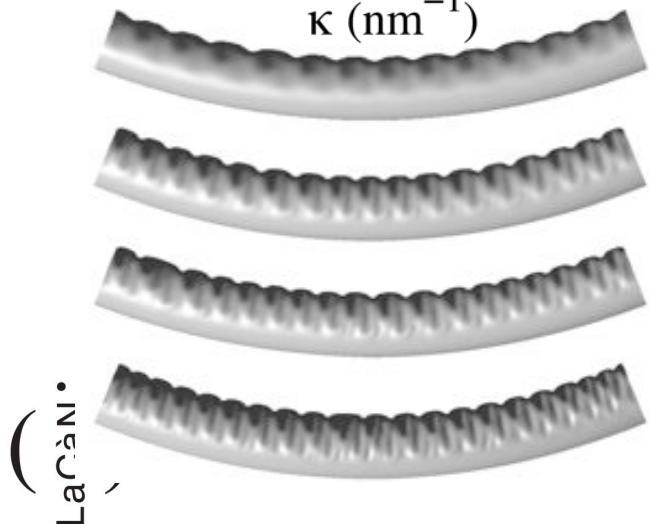
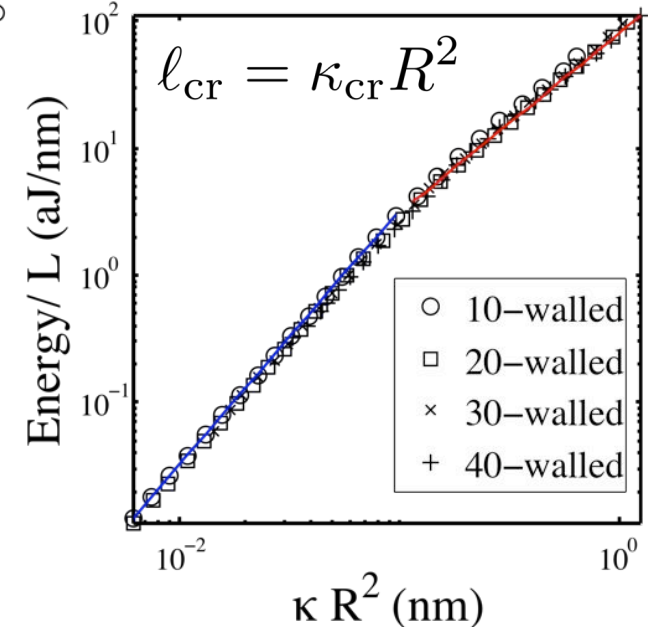
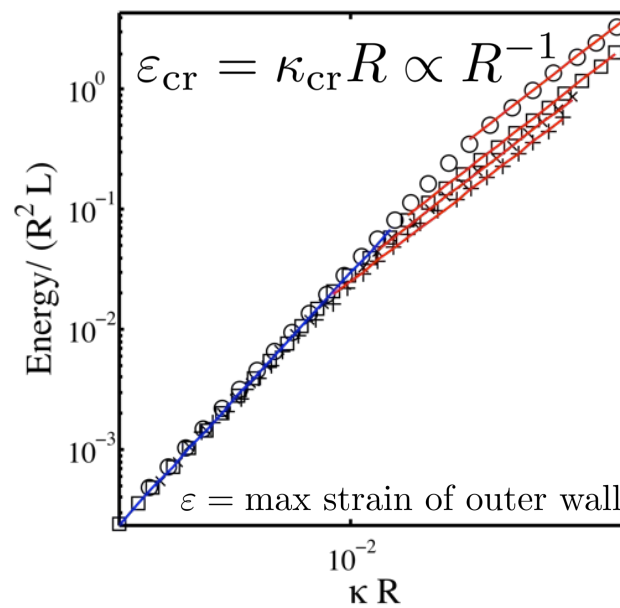
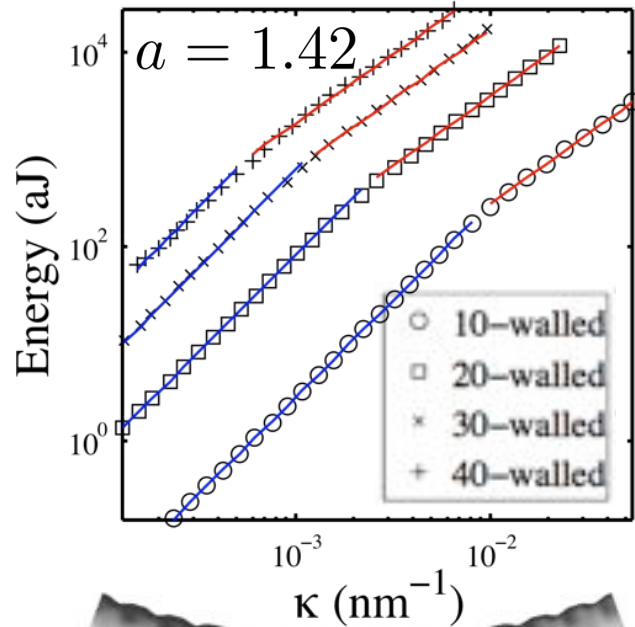
Mechanics of thick MWCNTs

The anharmonic exponent does not depend on the MWCNT diameter
 The usual non-dimensional scaling collapses only the **harmonic** response.



Mechanics of thick MWCNTs

Universal bending law: upon appropriate scaling we find data collapse for all the tested tubes. The law is characterized by three parameters.



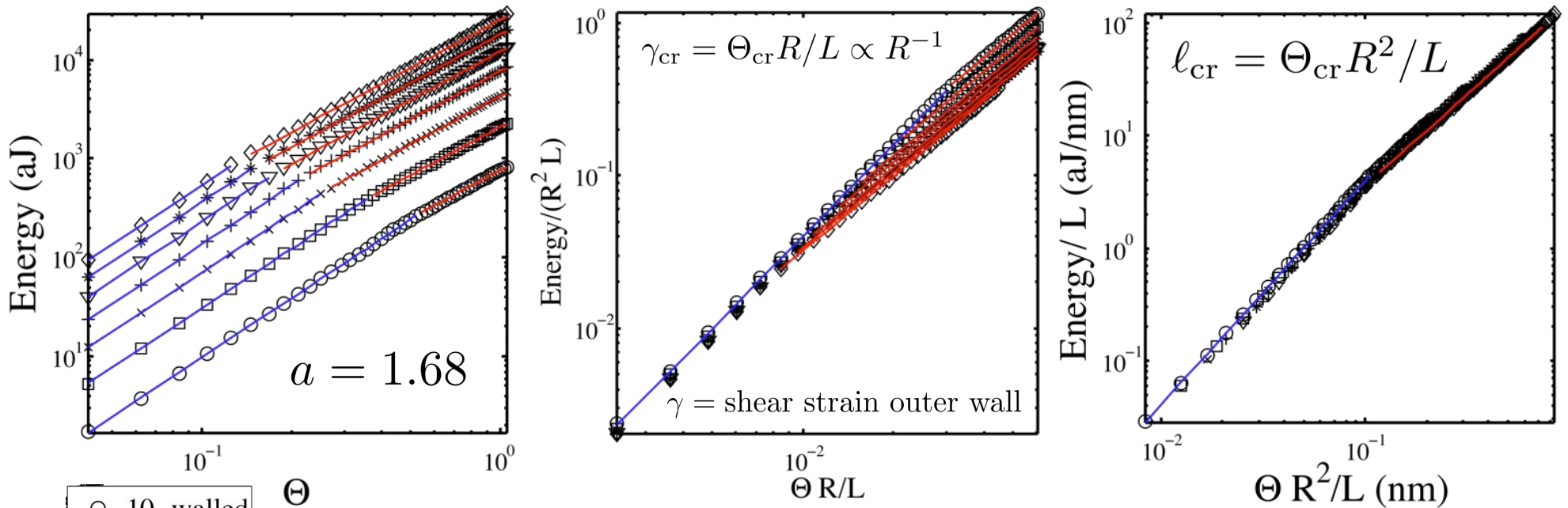
Size effect. the rescaling introduces a critical lengthscale l_{cr} : **thicker tubes ripple earlier**

$$w(\kappa) = \pi Y_s / (8t) \begin{cases} (\kappa R^2)^2 & \text{for } |\kappa R^2| \leq l_{\text{cr}} \\ l_{\text{cr}}^{2-a} |\kappa R^2|^a & \text{for } |\kappa R^2| > l_{\text{cr}} \end{cases}$$



Mechanics of thick MWCNTs

MWCNTs in torsion exhibit a **universal law** upon appropriate scaling with a **strong size-effect** (the scaling introduces a lengthscale).

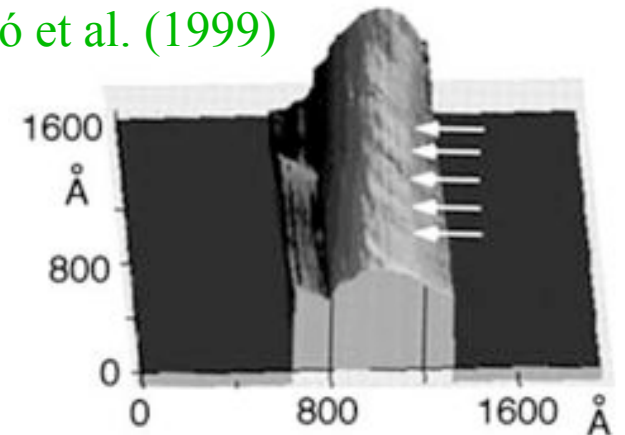


- 10-walled
- 15-walled
- × 20-walled
- + 25-walled
- ▽ 30-walled
- * 35-walled
- ◇ 40-walled

(LaCàN)



Forró et al. (1999)



Mechanics of thick MWCNTs

Both for torsion and bending, we find $l_{cr} \sim 0.1$ nm

	Prediction based on measurements	Actual observations
45-walled in bending [1]	$R^2 \kappa = 0.6$ nm $> l_{cr}$	TEM image of rippled tube
45-walled in bending [1]	$R^2 \kappa = 0.2$ nm $> l_{cr}$	Indirect evidence of nonlinearity and softening
12-walled in bending [1]	$R^2 \kappa = 0.05$ nm $< l_{cr}$	TEM image of smoothly bent tube
18 to 50-walled in torsion [2]	$R\gamma = 0.12$ nm $> l_{cr}$	Indirect evidence of nonlinearity

[1] Poncharal et al, *Science* (1999)

[2] Papadakis et al, *Phys. Rev. Lett.* (2004)

From experiments by Wong et al., *Science* (1997) $l_{cr} \sim 0.18$ nm

Multiple-scale analysis

Continuum surface models from atomistic models Arroyo & Belytschko, JMPS (2002)

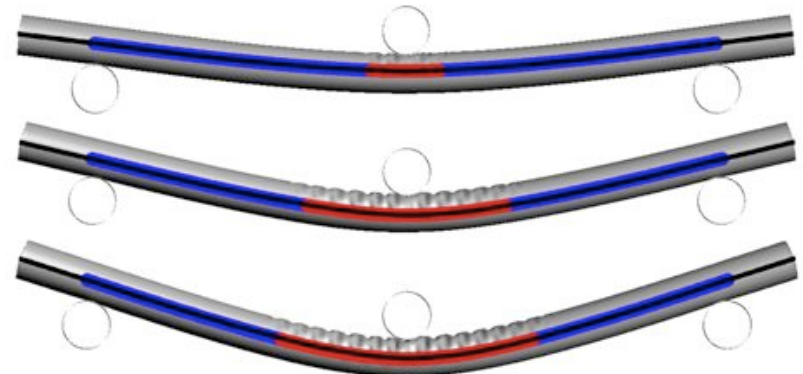
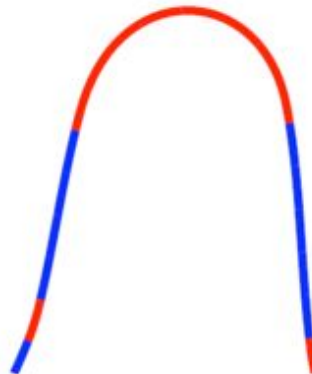


Mechanics of thick multiwalled CNTs through scaling laws



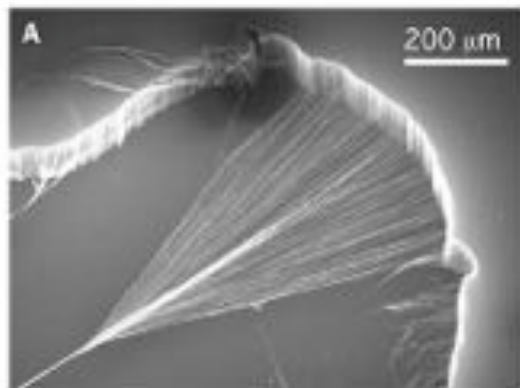
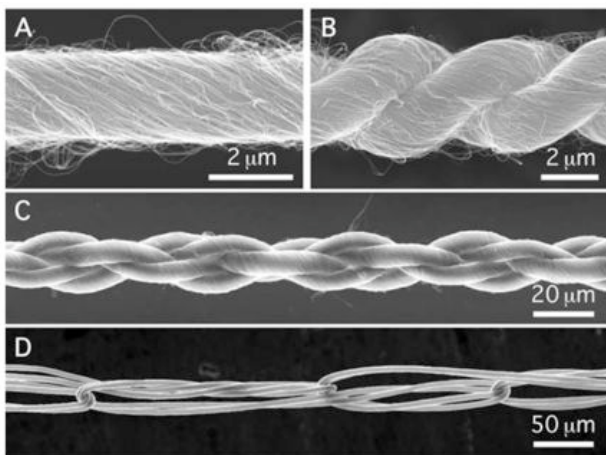
Mesoscopic models, phase-transforming elastica

(LaCàN•)

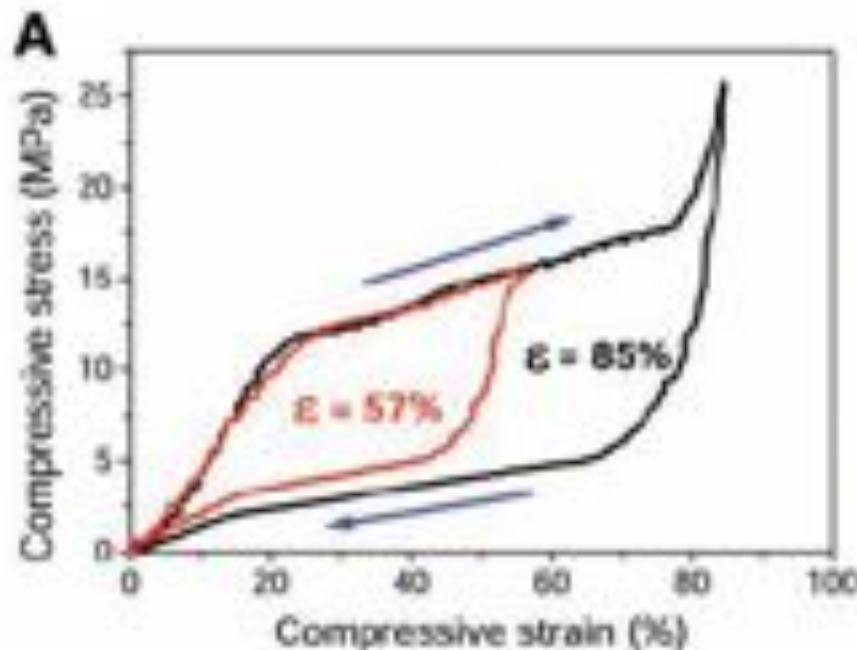
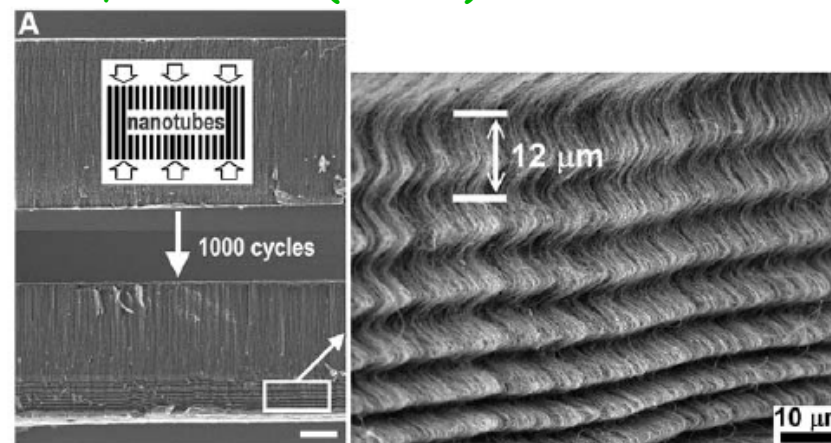


Mesoscopic model for thick MWCNTs

Textile technology
Zhang et al, Science (2004)



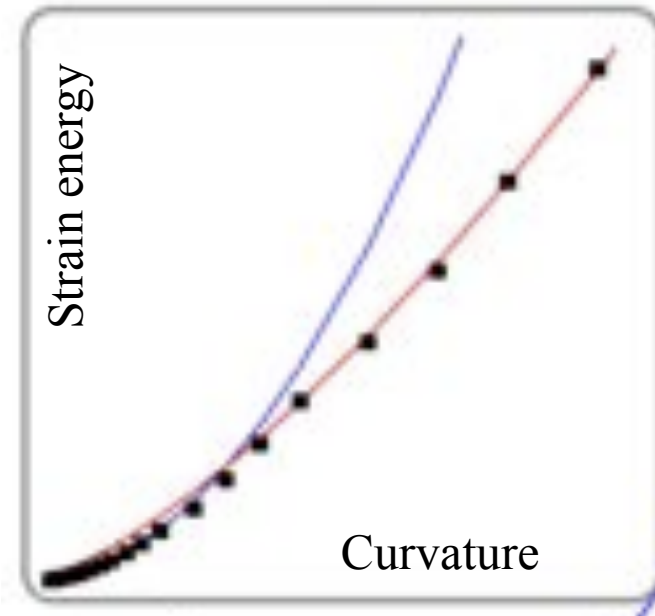
Supercompressible foam-like MWCNT films
Cao et al, Science (2005)



Mesoscopic model for thick MWCNTs

We have seen that for uniform bending, the strain energy per unit length follows

$$w(\kappa) = \min \left\{ \frac{1}{2} B \kappa^2; C \kappa^a \right\}$$



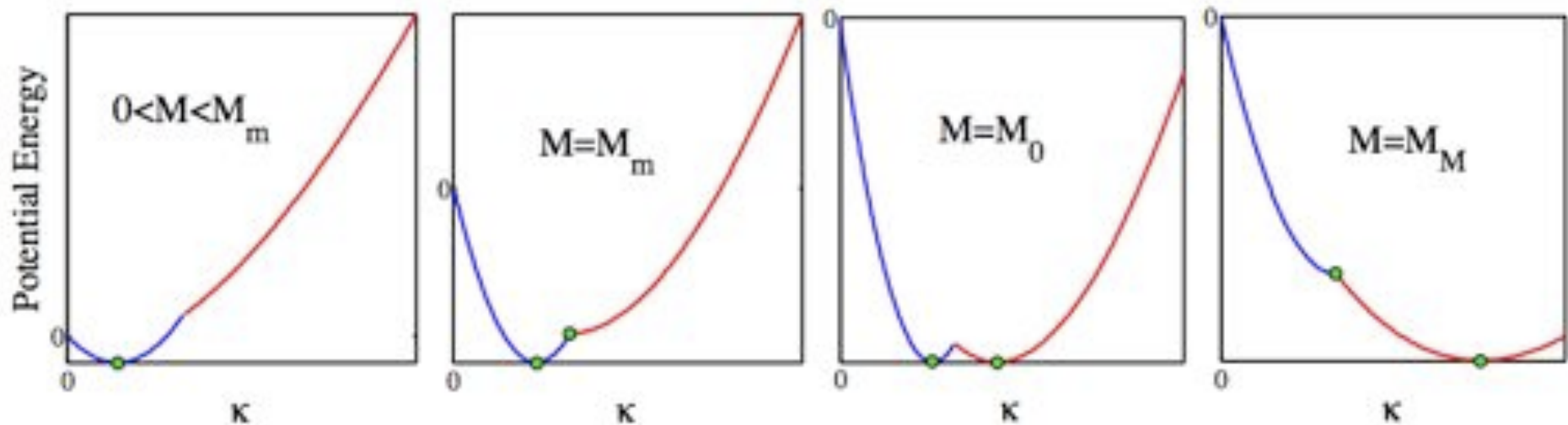
We can understand this as constitutive material response for a nonlinear beam?

M. Arroyo and I. Arias, *J. Mech. Phys. Solids* (2008).

Mesoscopic model for thick MWCNTs

Non-convex energy leads to phase mixtures, a **high strain phase (rippled)** and a **low-strain phase (smoothly bent)** (*Abeyaratne&Knowles, 2006*),

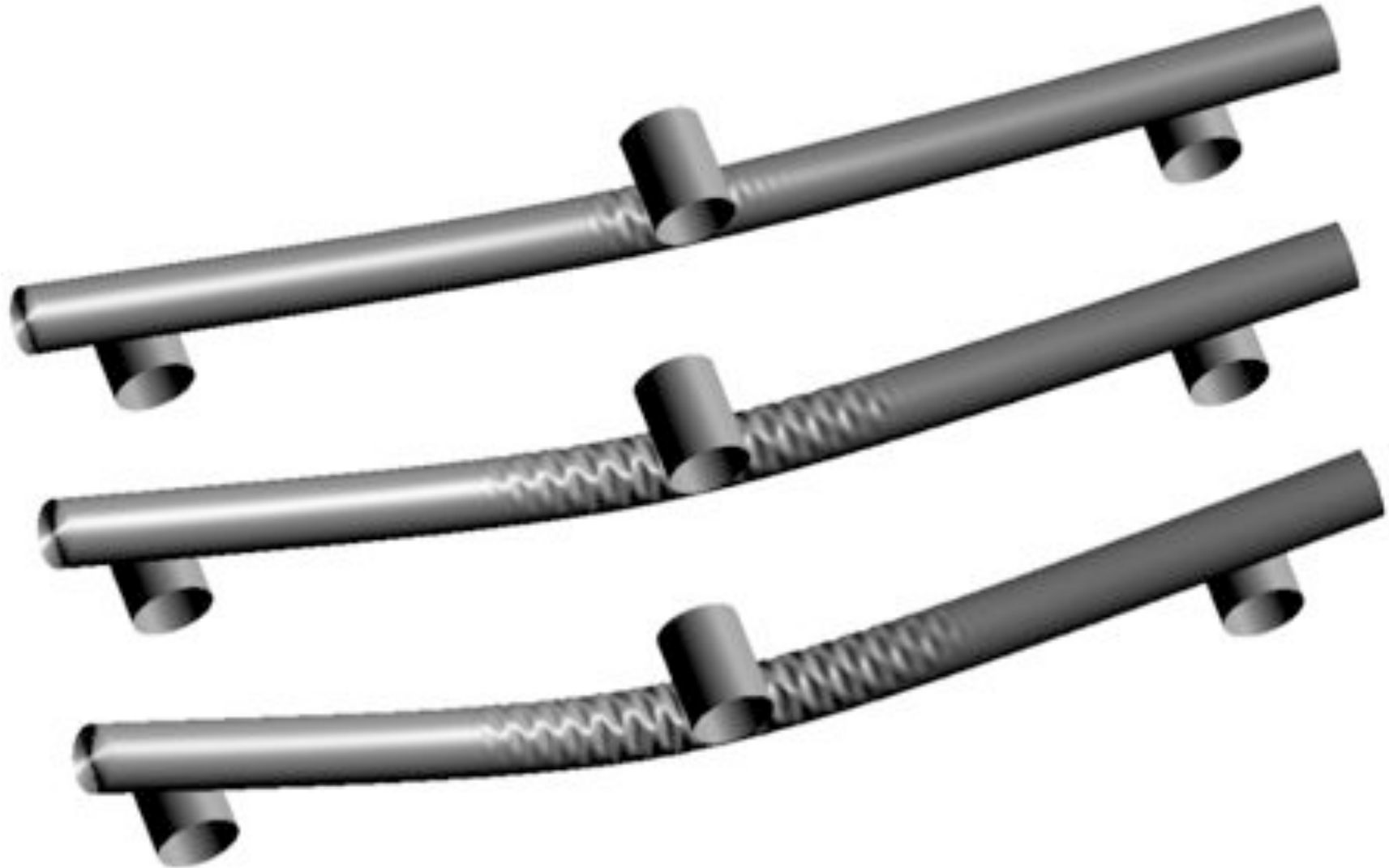
$$P(\kappa, M) = \min \left\{ \frac{1}{2} B \kappa^2; C \kappa^a \right\} - M \kappa$$



M. Arroyo and I. Arias, J. Mech. Phys. Solids (2008).

Mesoscopic model for thick MWCNTs

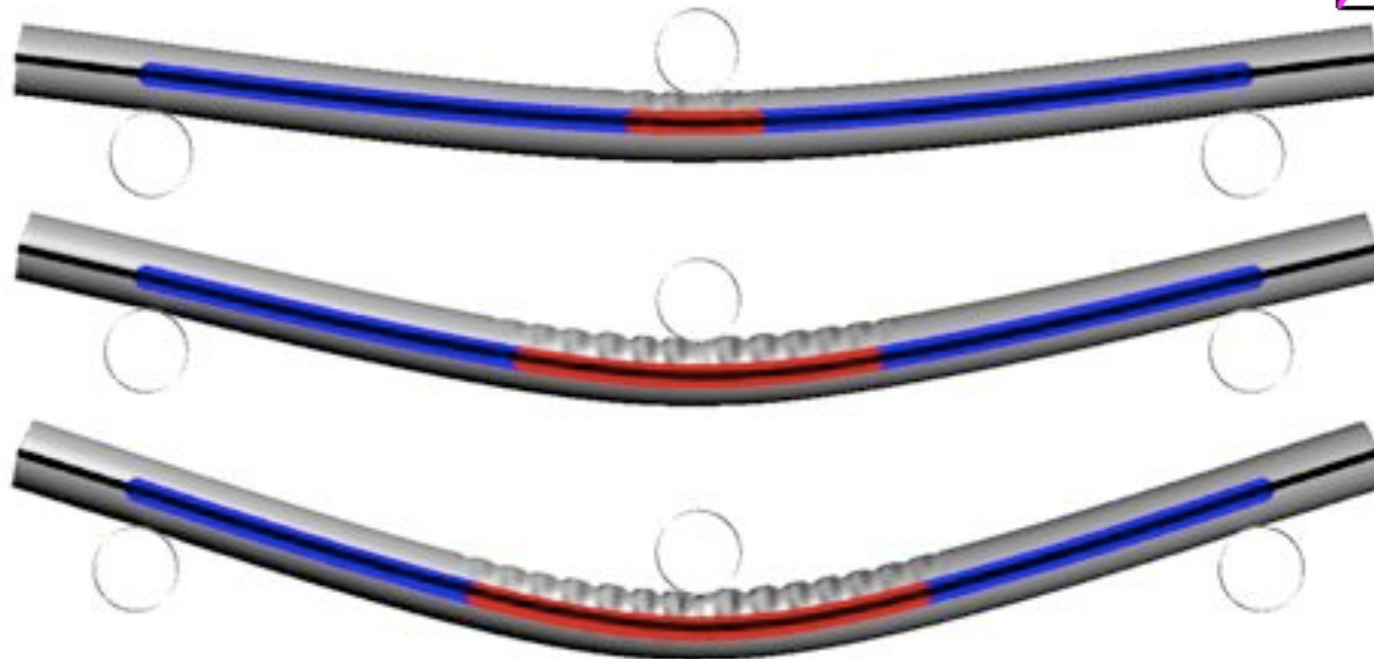
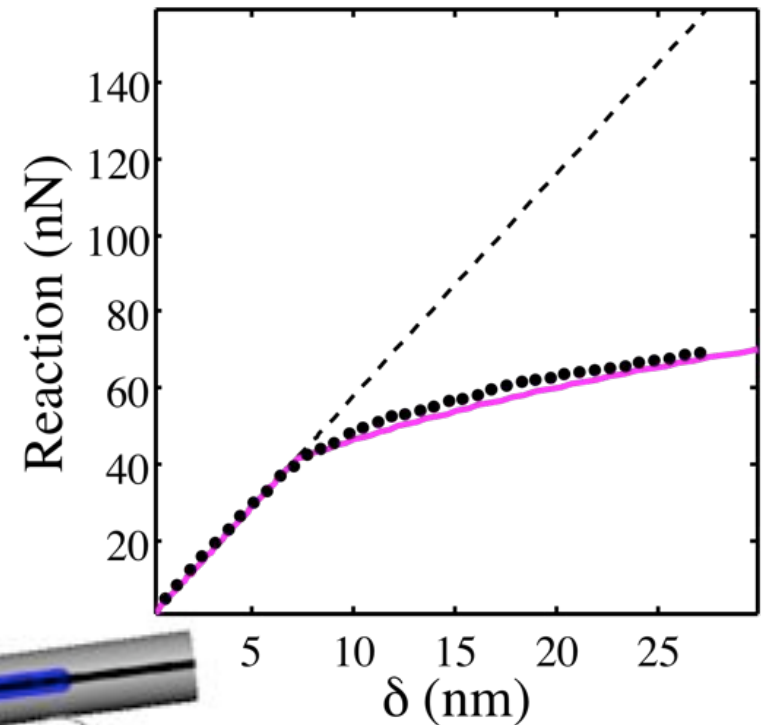
Three point bending of a 280 nm long 20-walled CNT



Mesososcopic model for thick MWCNTs

Validation of the model solved analytically against 3D simulations for 20-walled tube (1/2 million dofs)

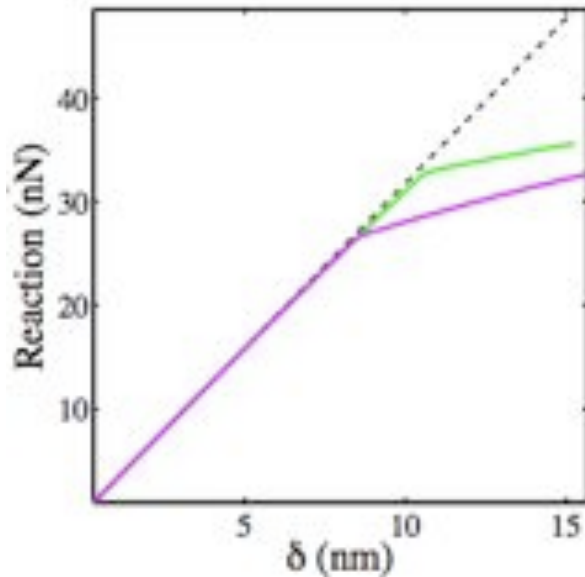
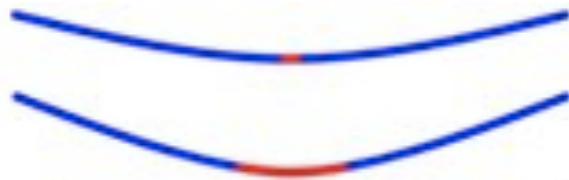
Actual force is less than half the force with harmonic beam



Mesoscopic model for thick MWCNTs

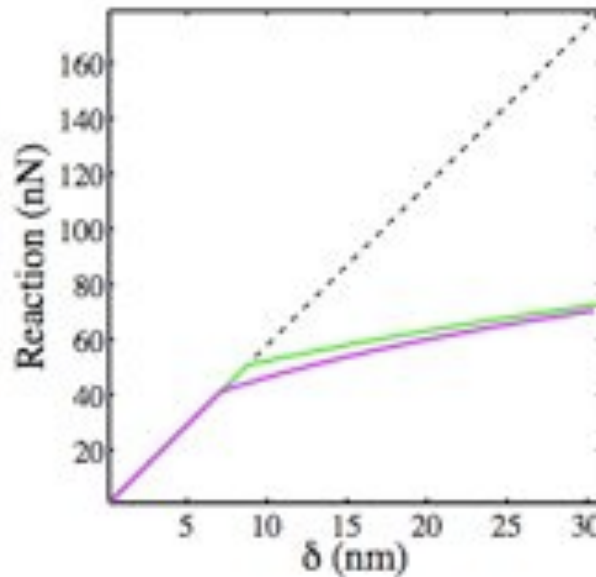
Size effect: *"Thicker tubes ripple earlier and appear softer"*

10-walled CNT 140 nm long



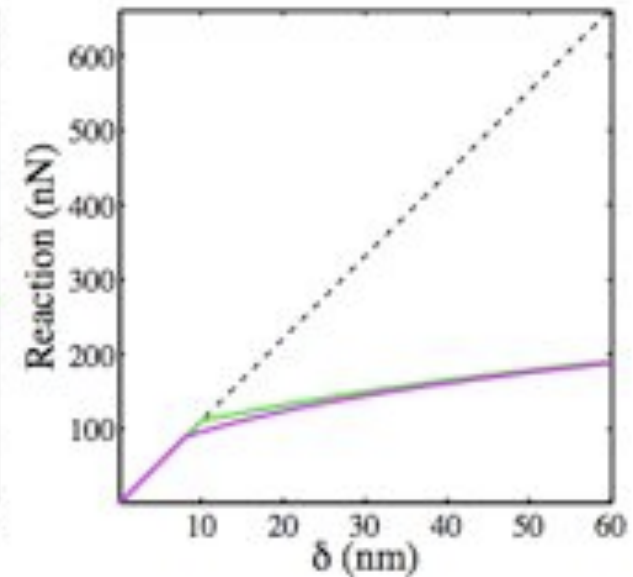
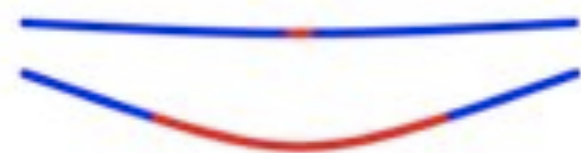
66% of elastic load

20-walled CNT 280 nm long



40% of elastic load

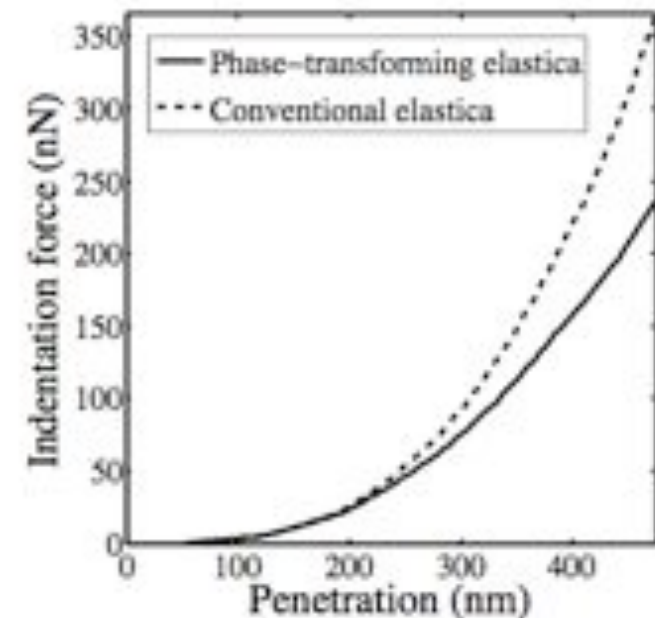
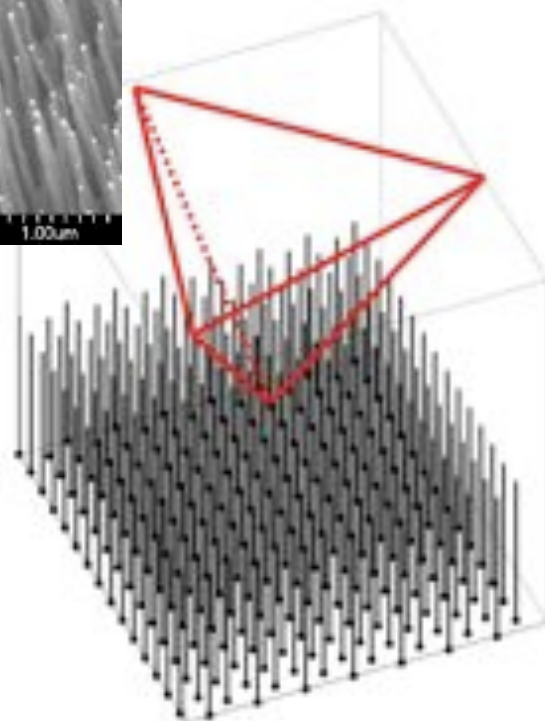
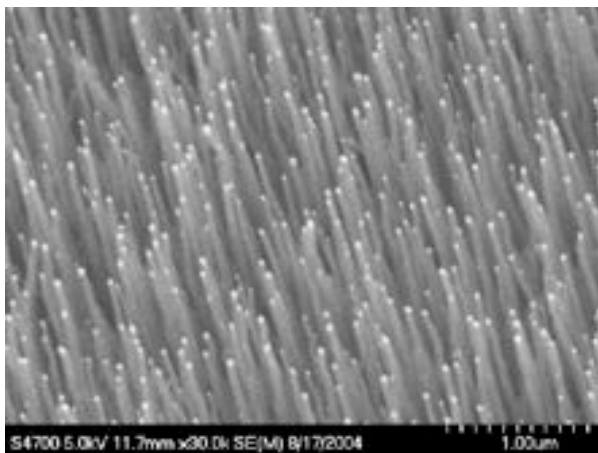
40-walled CNT 560 nm long



28% of elastic load

Mesososcopic model for thick MWCNTs

Nano-indentation of forests of vertically aligned MWCNTs forests, following the successive contact model of Qi et al, *JMPS* (2003) (40-walled 500 micron long tubes, density 200 MWCNTs/square micron)



Summary

- We have presented a multiple-scale modelling and simulation study of MWCNTs, from atomistic interactions up to engineering scales.
- MWCNTs are prone to rippling, both in bending and torsion.
- A universal scaling law (a composite power law) has been identified, which results in **strong size effect: *thicker tubes are softer***.
- The super-stiff response of MWCNTs is lost for thick tubes undergoing moderate deformation subject to other than pure tension.
- MWCNTs exhibit mixtures of rippled and smoothly bend regions, as a consequence of the non-convexity of the strain energy.
- The structural behavior is strongly hysteretic, with high energy dissipation in deformation cycles: tough energy-absorbing materials.