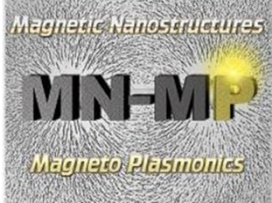




**CSIC**  
CONSEJO SUPERIOR DE INVESTIGACIONES CIENTÍFICAS



# Optical Chirality in the Stacked 3D Nanoring/Split Ring

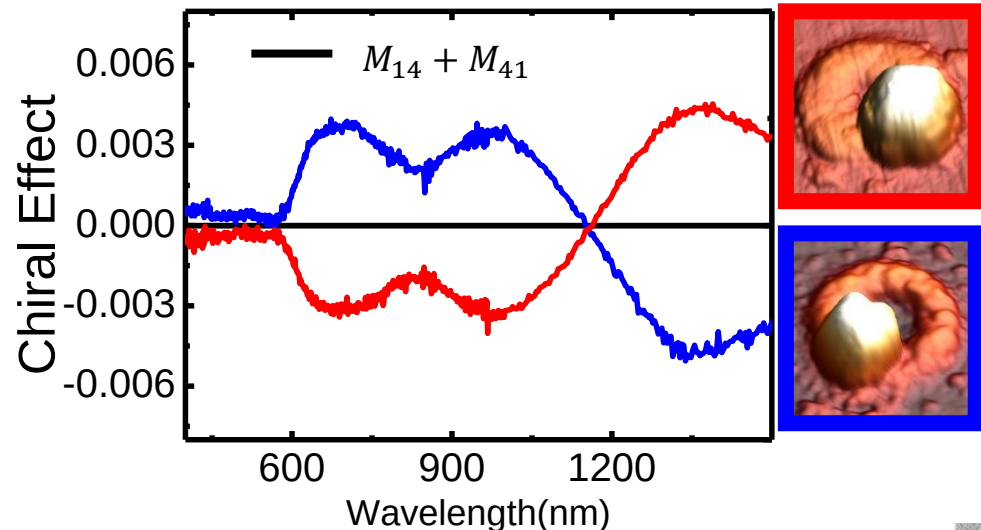
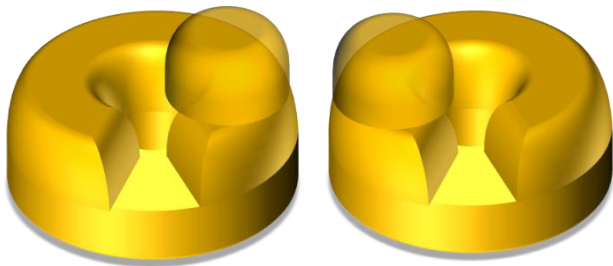
Hua Yu Feng, Carolina de Dios Fernández, Fernando García,  
Alfonso Cebollada, Gaspar Armelles



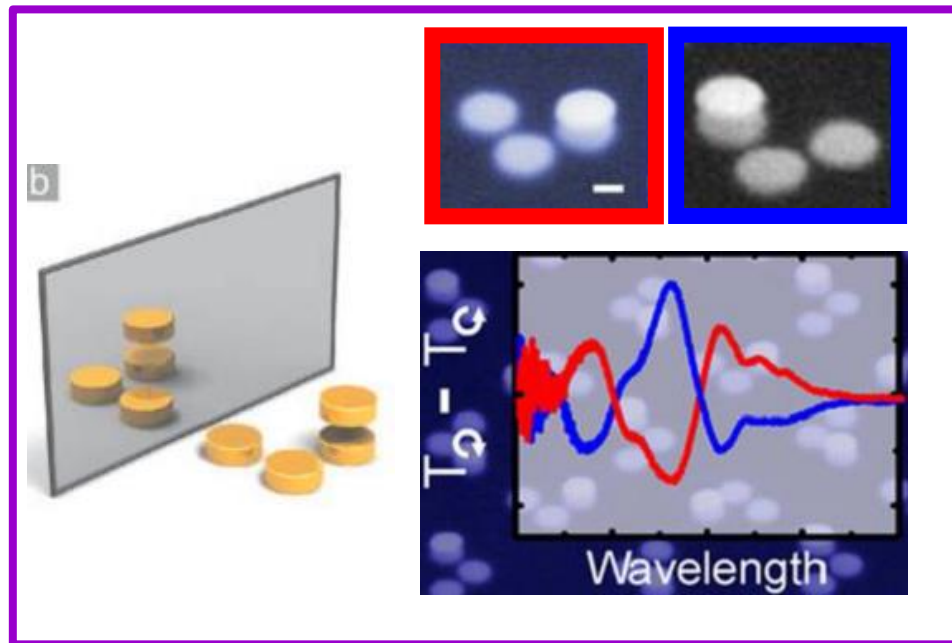
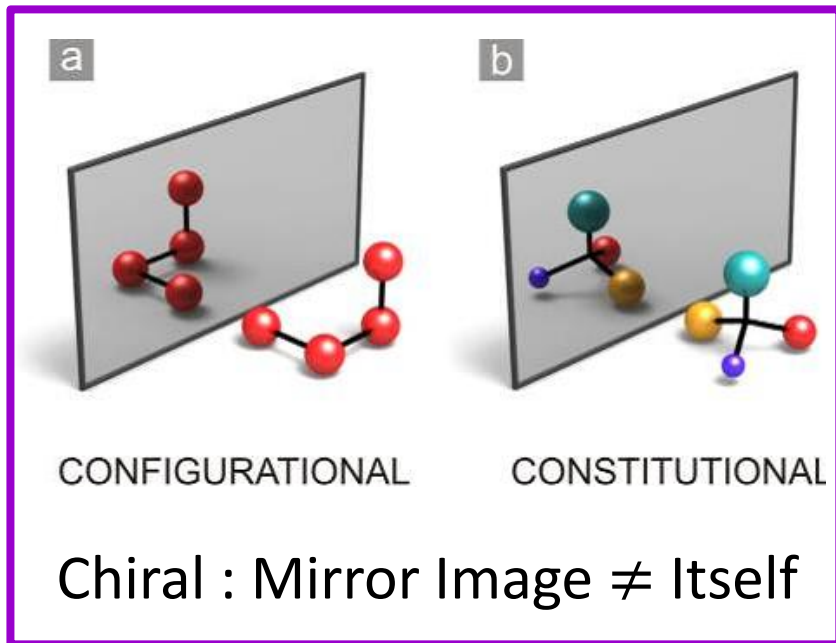
March 07-10, 2017 — San Sebastian (Spain)

# Outline

- 3D Chiral Stacked Ring/Split Ring
- Mueller Matrix for Chiral Effect
- Optical Chirality in the 3D Nanostructure



# 3D Chiral Stacked Ring/Split Ring



Our Purpose:

Chiral Effect in **Visible and NIR**

Future: **Magnetism + Chirality**

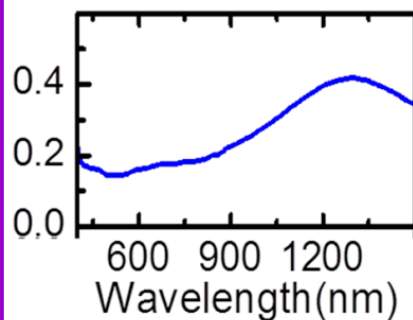
M. Hentschel, et al, Nano Lett. **12**, 2542.

# 3D Chiral Stacked Ring/Split Ring

Non-chiral



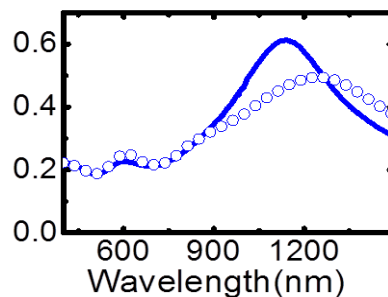
Extinction



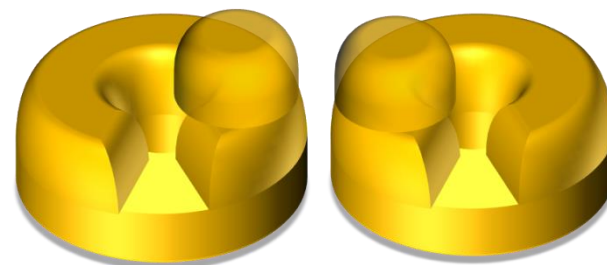
Non-chiral  
Optical Anisotropy



Extinction



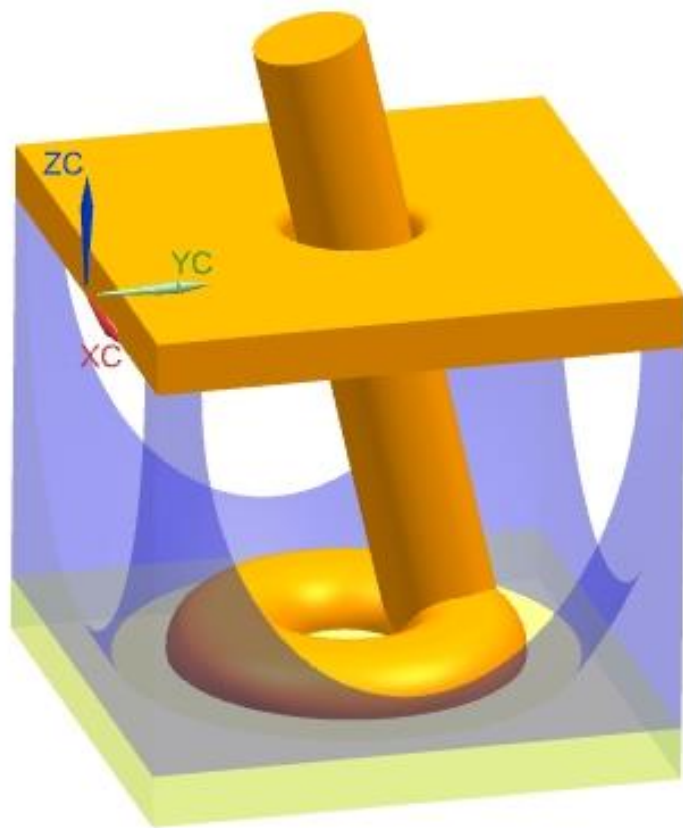
Chiral



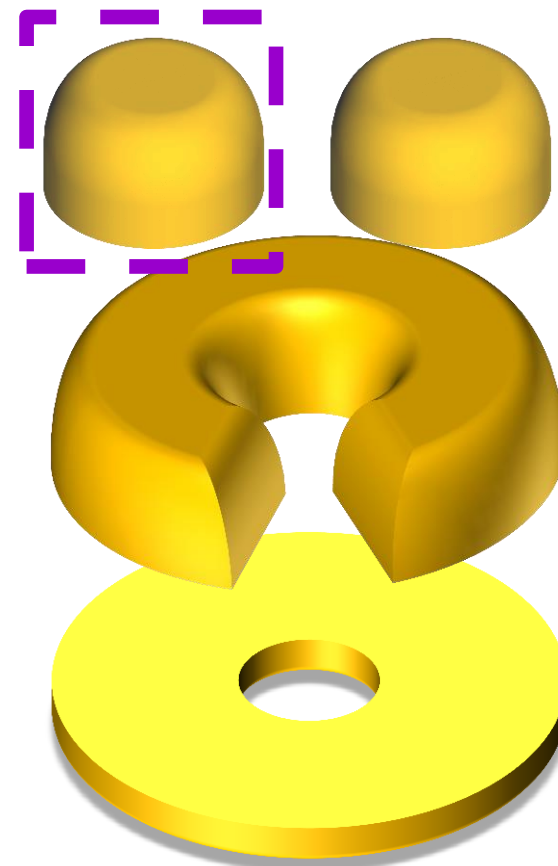
Split ring  
Disk  
Gap



## 3D Chiral Stacked Ring/Split Ring

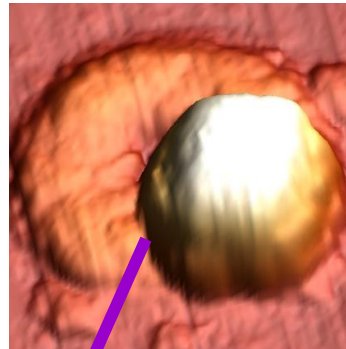
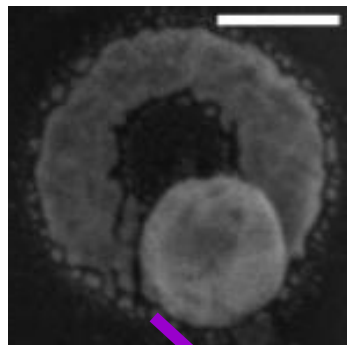


Hole-mask  
Colloidal Lithography

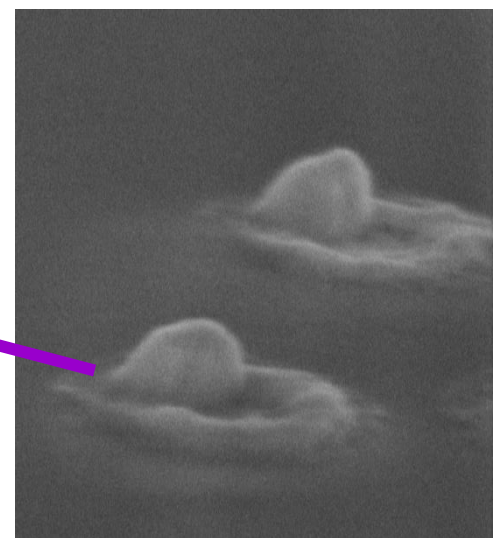
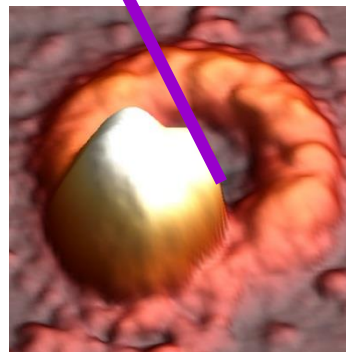
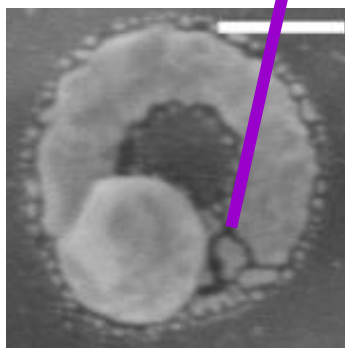




## 3D Chiral Stacked Ring/Split Ring



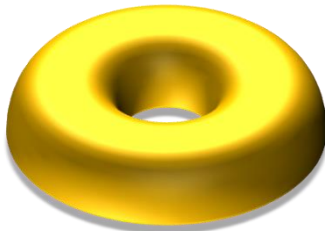
**Gap**



Scale bar: **100nm**

# Mueller Matrix for Chiral Effect

In-plane Isotropy  
Non-chiral



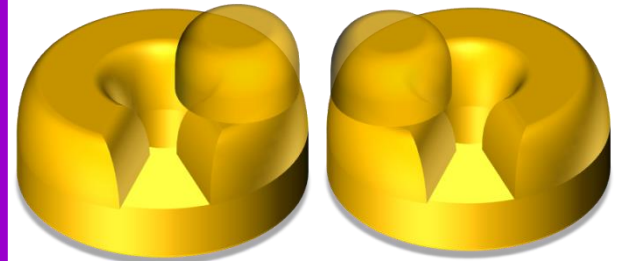
$$\begin{pmatrix} t_{xx} & 0 \\ 0 & t_{xx} \end{pmatrix}$$

Optical Anisotropy  
Non-chiral



$$\begin{pmatrix} t_{xx} & 0 \\ 0 & t_{yy} \end{pmatrix}$$

Optical Anisotropy  
Chiral

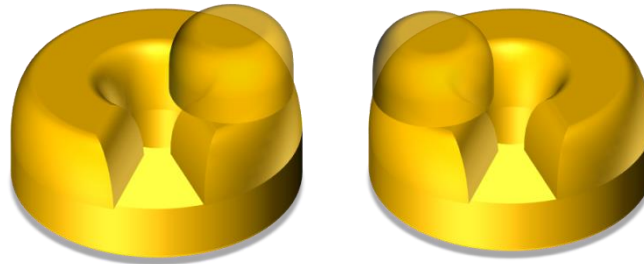


$$\begin{pmatrix} t_{xx} & t_{xy} \\ t_{yx} & t_{yy} \end{pmatrix}$$

$$t_{xy} \neq t_{yx}$$

**Jones  
Matrix**

# Mueller Matrix for Chiral Effect



$$\begin{pmatrix} t_{xx} & t_{xy} \\ t_{yx} & t_{yy} \end{pmatrix} \xrightarrow{t_{xy} \neq t_{yx}} \begin{pmatrix} t_{xx} & t_{sy} + t_a \\ t_{sy} - t_a & t_{yy} \end{pmatrix}$$

**“Optical Anisotropy”**  $t_{sy} = \frac{1}{2}(t_{xy} + t_{yx})$

**Chiral effect**  $t_a = \frac{1}{2}(t_{xy} - t_{yx})$

**How to obtain???**



# Mueller Matrix for Chiral Effect

## Jones Matrix

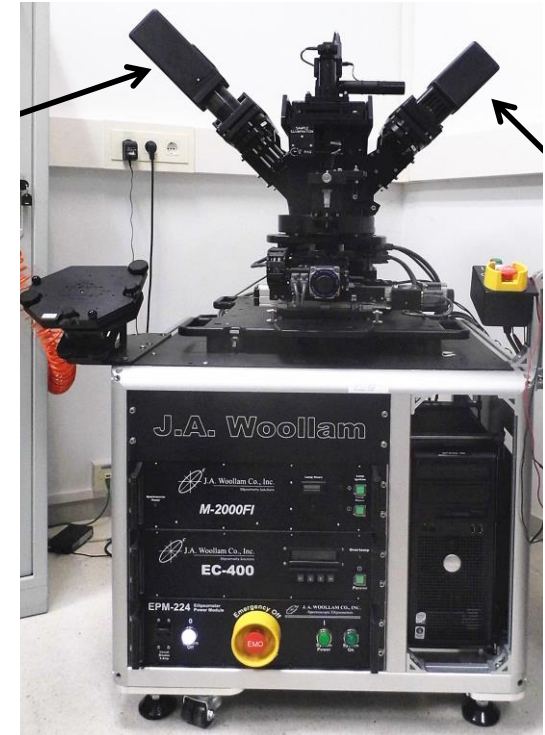
$$\begin{pmatrix} t_{xx} & t_{sy} + t_a \\ t_{sy} - t_a & t_{yy} \end{pmatrix}$$

## Mueller Matrix

$$\begin{pmatrix} M_{11} & M_{12} & M_{13} & M_{14} \\ M_{21} & M_{22} & M_{23} & M_{24} \\ M_{31} & M_{32} & M_{33} & M_{34} \\ M_{41} & M_{42} & M_{43} & M_{44} \end{pmatrix}$$

$$M_{14} = -\text{Im} \left( (t_{xx}^* - t_{yy}^*) t_{sy} \right) - \text{Im} \left( (t_{xx}^* + t_{yy}^*) t_a \right)$$

$$M_{41} = \text{Im} \left( (t_{xx}^* - t_{yy}^*) t_{sy} \right) - \text{Im} \left( (t_{xx}^* + t_{yy}^*) t_a \right)$$



H. Fujiwara, *Spectroscopic Ellipsometry: Principles and Applications* (John Wiley & Sons, 2007)

# Mueller Matrix for Chiral Effect

## CD: Circular Dichroism

$$\sim \frac{I_{LCP} - I_{RCP}}{I_{LCP} + I_{RCP}}$$

$$M_{14} = -\text{Im} \left( (t_{xx}^* - t_{yy}^*) t_{sy} \right) - \text{Im} \left( (t_{xx}^* + t_{yy}^*) t_a \right)$$

$$M_{41} = \text{Im} \left( (t_{xx}^* - t_{yy}^*) t_{sy} \right) - \text{Im} \left( (t_{xx}^* + t_{yy}^*) t_a \right)$$



$$M_{14} + M_{41} = -2\text{Im} \left( (t_{xx}^* + t_{yy}^*) t_a \right) \sim \frac{I_{LCP} - I_{RCP}}{I_{LCP} + I_{RCP}}$$

## Optical Activity

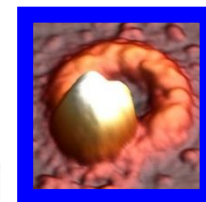
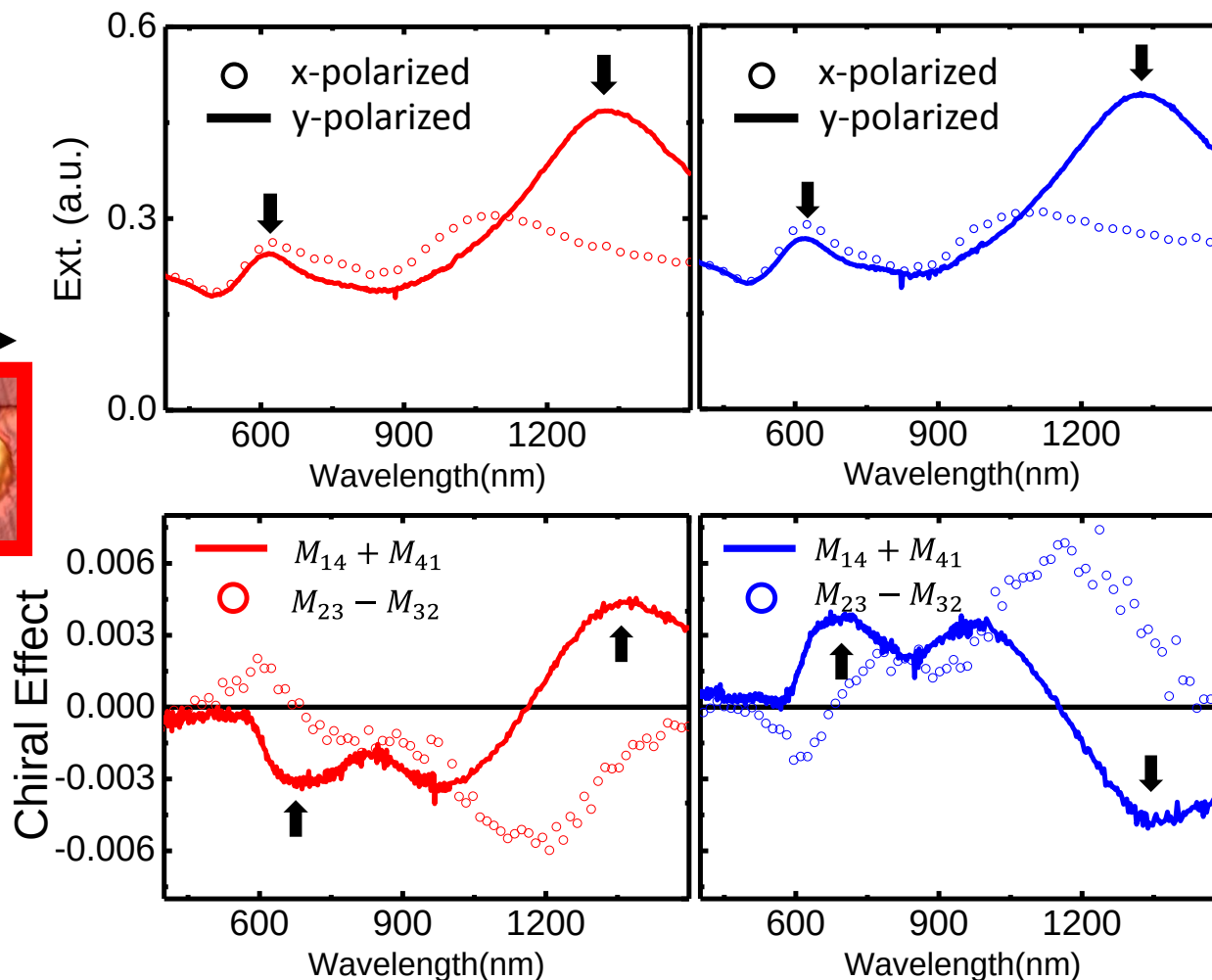
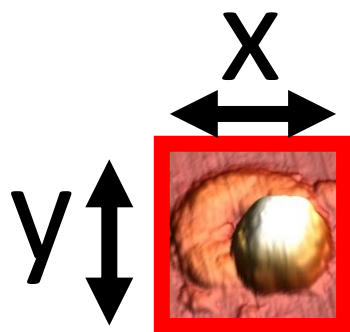
$$M_{23} = \text{Re} \left( (t_{xx} - t_{yy}) t_{sy}^* \right) + \text{Re} \left( (t_{xx} + t_{yy}) t_a^* \right)$$

$$M_{32} = \text{Re} \left( (t_{xx} - t_{yy}) t_{sy}^* \right) - \text{Re} \left( (t_{xx} + t_{yy}) t_a^* \right)$$



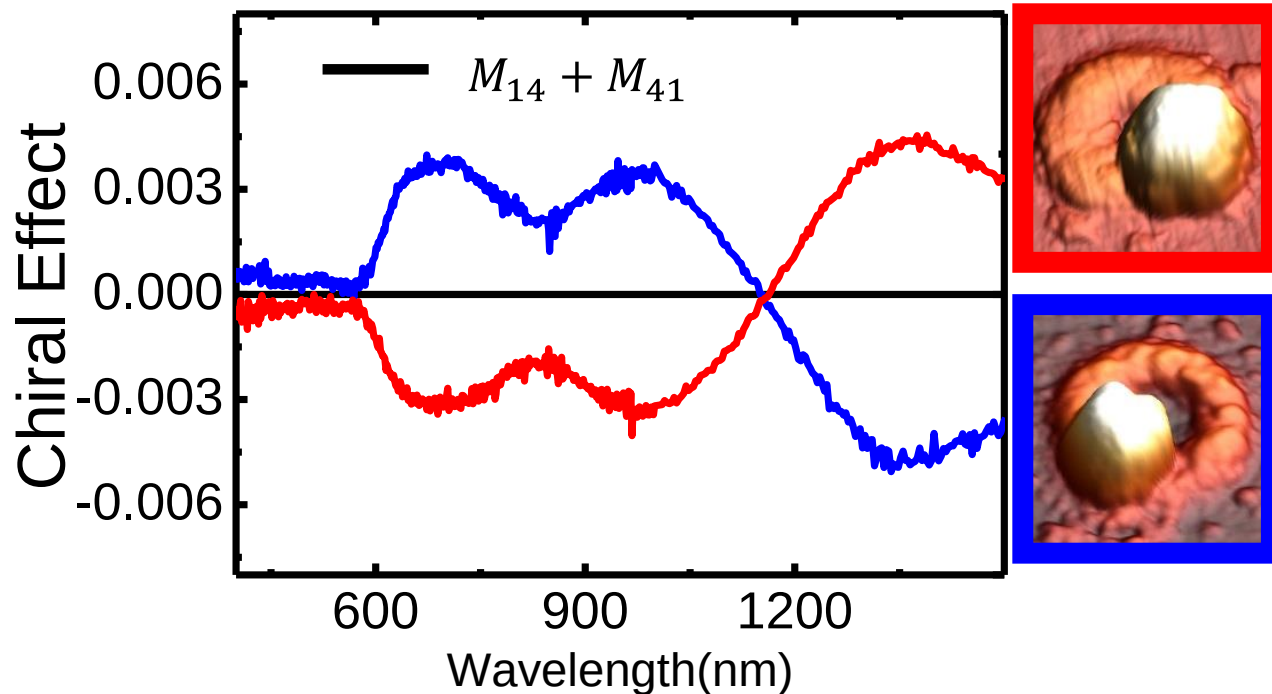
$$M_{23} - M_{32} = 2\text{Re} \left( (t_{xx} + t_{yy}) t_a^* \right)$$

# Chiral Effects in the 3D Nanostructure

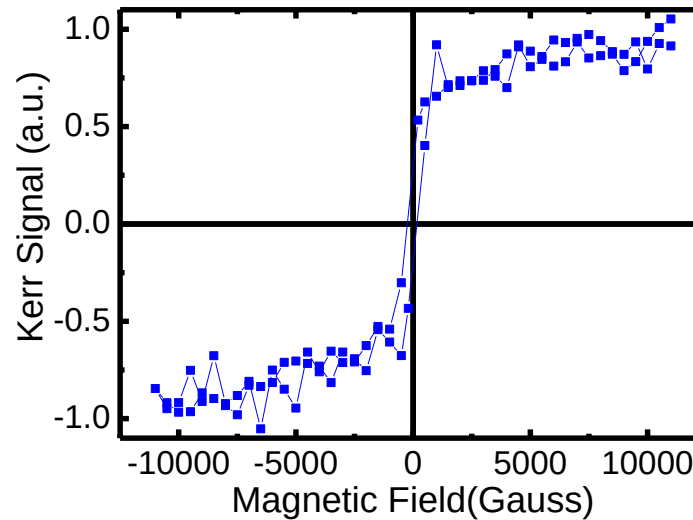
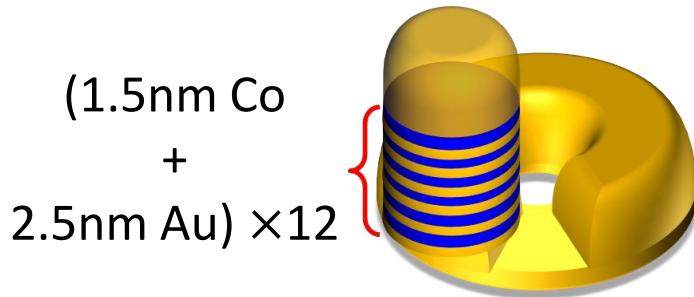


# Chiral Effects in the 3D Nanostructure

$$CD = \frac{1}{2} (M_{14} + M_{41}) = \frac{I_{LCP} - I_{RCP}}{I_{LCP} + I_{RCP}}$$

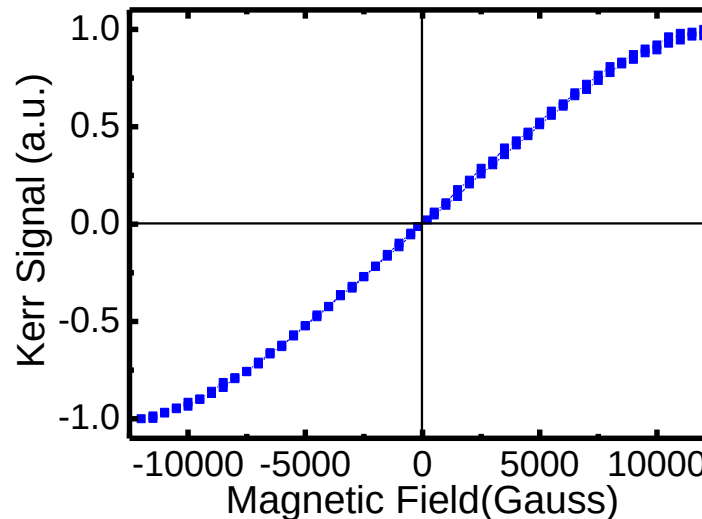


# Magnetism + Chirality ?



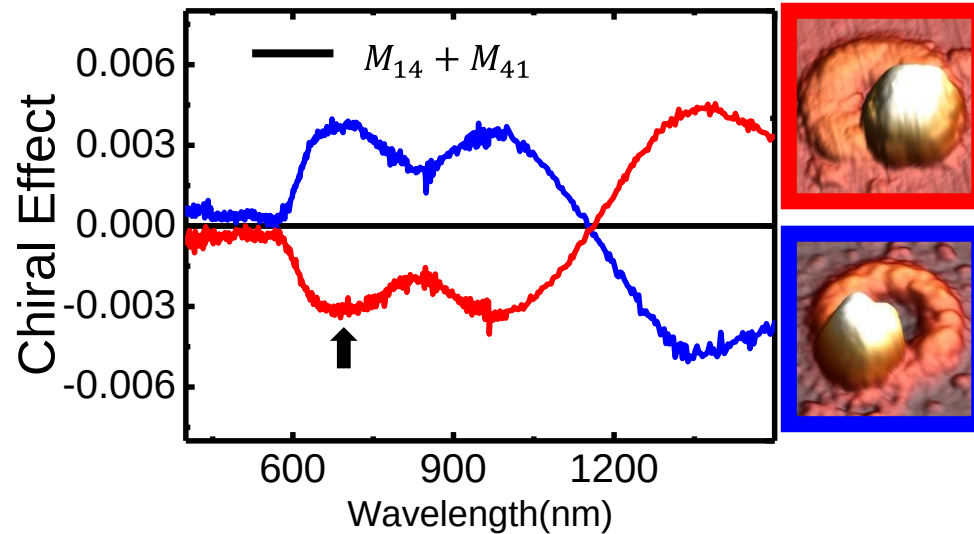
Out-of-plane loop

Perpendicular  
Magnetic  
Anisotropy

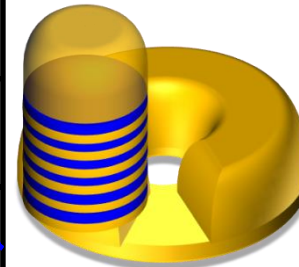
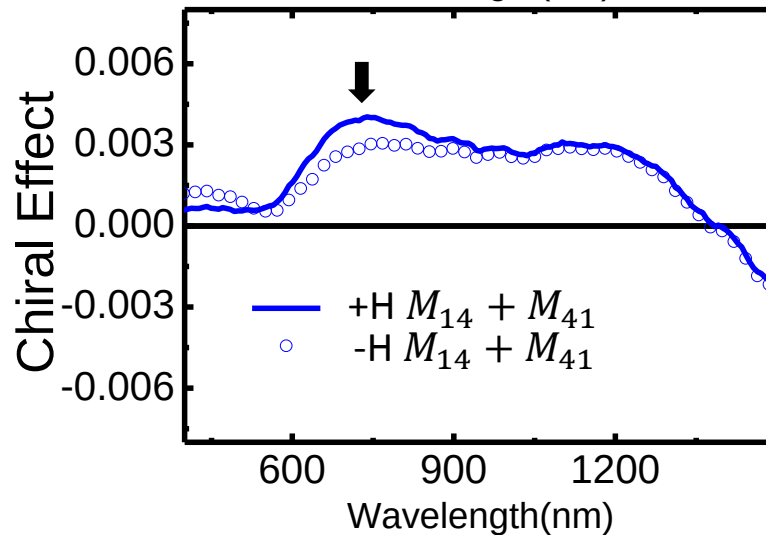


# Magnetism + Chirality ?

No Co



With Co  
 $\pm H$



H field:  $\sim 3000$ Gauss

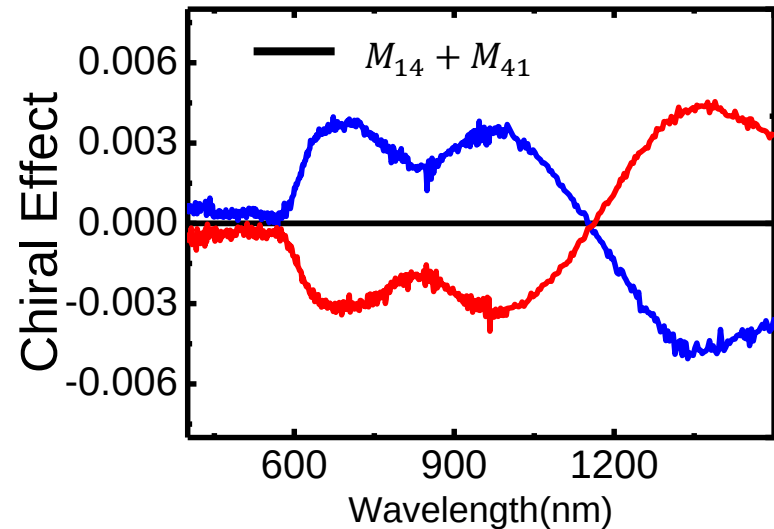
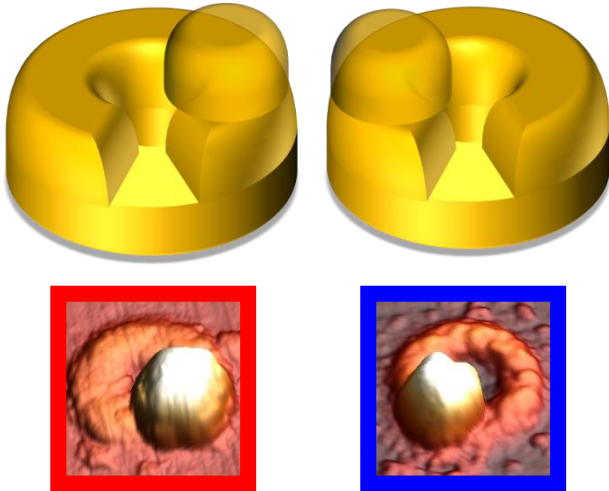


# Conclusions

3D Chiral  
Stacked Ring/Split Ring



Mueller Matrix



## Thank you!

# Acknowledgement

We acknowledge funding from the Spanish MINECO (CSD2008-00023, MAT2014-58860-P).

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## Thank you!